



**QUEEN'S  
UNIVERSITY  
BELFAST**

## **Power Allocation for Energy Efficiency and Secrecy of Wireless Interference Networks**

Sheng, Z., Tuan, H. D., Nasir, A. A., Duong, Q., & Poor, H. V. (2018). Power Allocation for Energy Efficiency and Secrecy of Wireless Interference Networks. *IEEE Trans on Wireless Communications*, 17(6), 3737-3751. <https://doi.org/10.1109/TWC.2018.2815626>

**Published in:**  
IEEE Trans on Wireless Communications

**Document Version:**  
Peer reviewed version

**Queen's University Belfast - Research Portal:**  
[Link to publication record in Queen's University Belfast Research Portal](#)

### **Publisher rights**

© 2018 IEEE. This work is made available online in accordance with the publisher's policies. Please refer to any applicable terms of use of the publisher.

### **General rights**

Copyright for the publications made accessible via the Queen's University Belfast Research Portal is retained by the author(s) and / or other copyright owners and it is a condition of accessing these publications that users recognise and abide by the legal requirements associated with these rights.

### **Take down policy**

The Research Portal is Queen's institutional repository that provides access to Queen's research output. Every effort has been made to ensure that content in the Research Portal does not infringe any person's rights, or applicable UK laws. If you discover content in the Research Portal that you believe breaches copyright or violates any law, please contact [openaccess@qub.ac.uk](mailto:openaccess@qub.ac.uk).

# Power Allocation for Energy Efficiency and Secrecy of Wireless Interference Networks

Zhichao Sheng, Hoang Duong Tuan, Ali Arshad Nasir, Trung Q. Duong and H. Vincent Poor

**Abstract**—Considering a multi-user interference network with an eavesdropper, this paper aims at the power allocation to optimize the worst secrecy throughput among the network links or the secure energy efficiency in terms of achieved secrecy throughput per Joule under link security requirements. Three scenarios for the access of channel state information are considered: the perfect channel state information, partial channel state information with channels from the transmitters to the eavesdropper exponentially distributed, and not perfectly known channels between the transmitters and the users with exponentially distributed errors. The paper develops various path-following procedures of low complexity and rapid convergence for the optimal power allocation. Their effectiveness and viability are illustrated through numerical examples. The power allocation schemes are shown to achieve both high secrecy throughput and energy efficiency.

**Index Terms**—Interference network, secure communication, energy-efficient communication, power allocation, path-following algorithms.

## I. INTRODUCTION

The broadcast nature of the wireless medium exhibits different challenges in ensuring secure communications in the presence of adversarial users [1], [2]. In particular, it is difficult to protect the transmitted signals from unintended recipients, who may improperly extract information from an ongoing transmission without being detected [3], [4]. Physical layer security [5], [6] has been proposed as a solution to provide security in wireless networks and researchers with a goal being to optimize the secure throughput of a wireless network in the presence of eavesdroppers, which is the difference between the desired user throughput and eavesdroppers' throughput [2]. Beyond secure throughput, significant interest has recently been put on optimizing the secure energy efficiency (SEE), which is the ratio of the secure throughput to the total network power consumption, measured in terms of bits per Joule per Hertz [7], [8].

This work was supported in part by the Australian Research Council's Discovery Projects under Project DP130104617, in part by King Fahd University of Petroleum and Minerals under Start-up Research Project #SR161003, in part by a U.K. Royal Academy of Engineering Research Fellowship under Grant RF1415/14/22, and in part by the U.S. National Science Foundation under Grants CNS-1702808 and ECCS-1647198

Zhichao Sheng and Hoang Duong Tuan are with the School of Electrical and Data Engineering, University of Technology Sydney, Broadway, NSW 2007, Australia (email: zhichaosheng@163.com, Tuan.Hoang@uts.edu.au)

Ali Arshad Nasir is with Department of Electrical Engineering, King Fahd University of Petroleum and Minerals (KFUPM), Dhahran, Saudi Arabia (email: anasir@kfupm.edu.sa)

Trung Q. Duong is with Queen's University Belfast, Belfast BT7 1NN, UK (email: trung.q.duong@qub.ac.uk)

H. Vincent Poor is with the Department of Electrical Engineering, Princeton University, Princeton, NJ 08544, USA (e-mail: poor@princeton.edu)

There has been considerable recent research on physical layer security in wireless communication systems. For example, assuming the availability of full channel state information (CSI), secrecy optimization has been studied for cooperative relaying networks in [9]–[11]. Energy efficiency (EE) of wireless networks has also drawn attention. For examples, resource allocation algorithms for the optimization of spectral efficiency as well as EE have been established in [12]. Keeping EE maximization as an objective, the authors in [13] proposed a precoder design for multi-input-multi-output (MIMO) two-way relay networks. EE maximization for cooperative spectrum sensing in cognitive sensor networks is studied in [14].

The critical topic of SEE has also been explored very recently [7], [8], [15]–[20]. Specifically, power control algorithms for SEE maximization in decode-and-forward (DF) and amplify-and-forward (AF) relaying networks have been considered in [15] and [7], respectively. In [16], the authors developed a distributed power control algorithm for SEE maximization in DF relaying. The same resource allocation problem for SEE maximization assuming full-duplex relaying is considered in [17]. Recently, the authors in [18] and [19] also derived the trade-off between SEE and secure spectral efficiency in cognitive radio networks, while the authors in [21] considered similar problems for ultra-dense small cells underlaid on macro cells. All these works have assumed the perfect CSI knowledge at the transmitter end, which is not always possible.

It is commonly known that time or frequency resources are generally limited in wireless networks and thus have to be shared among multiple users. This can result in interference among users in the network and thus one has to opt for careful resource allocation or interference alignment schemes [22]. Considering a multiuser MIMO interference network, [20] used the costly interference alignment technique to cancel both information leakage and interference and then Dinkelbach's method of fractional programming is adopted to optimize EE. As shown in [8], both zero-forcing and interference alignment are not efficient in optimizing the network SEE.

In this paper, we propose novel and efficient resource allocation algorithms for both worst-case secure throughput and worst secure energy efficiency maximization of a highly interference-limited multi-user wireless network. Unlike many previous works, we do not assume perfect CSI knowledge at the transmitters. In fact, our transmitters only carry channel distribution knowledge for the eavesdropper and imperfect CSI for the users. Particularly, we consider three optimization scenarios to gradually build our algorithms. We start with the “perfect CSI” scenario. Next, we consider a “partial CSI”

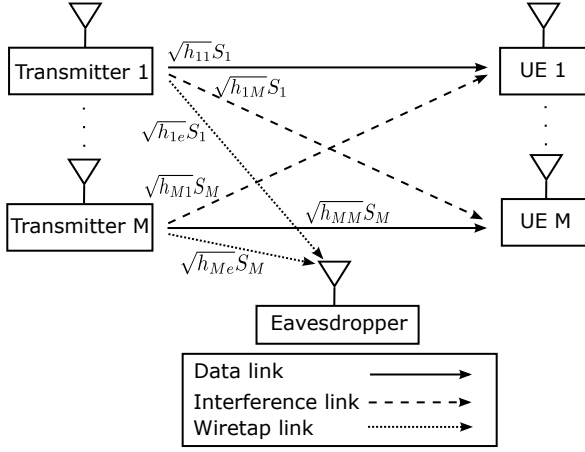


Fig. 1. System model

setup where the channel between the transmitters and the eavesdropper is exponentially distributed and only that channel distribution knowledge is available at the transmitters. Finally, we solve for the hardest “robust optimization” scenario, where in addition to the assumption of only channel distribution knowledge about eavesdroppers, we also assume uncertain channels between the transmitters and the users with exponentially distributed errors. We develop various path-following procedures of low complexity and rapid convergence for the optimal power allocation. Our extensive simulation results illustrate their effectiveness and viability.

The rest of the paper is organized as follows. Section II, section III and section IV are devoted to optimizing the links’ worst secrecy throughput and the network secure energy efficiency under the perfect CSI, partial CSI and imperfectly known CSI, respectively. The simulation is provided in Section V to show the efficiency of the theoretical developments in the previous section. Appendices provide fundamental rate outage inequalities and approximations, which are the mathematical base of the theoretical sections II-IV.

## II. INTERFERENCE NETWORKS UNDER PERFECT CSI

We consider a cooperative network consisting of  $M$  single-antenna transmitters and  $M$  single-antenna users as depicted in Figure 1, where each transmitter  $i$  intends to send the information  $s_i$  to user  $i$ . The information  $s_i$  is normalized, i.e.  $\mathbb{E}(x_i^2) = 1$ . Let  $\mathbf{p}_i$  be the transmit power allocated to transmitter  $i$  and  $\mathbf{p} = (\mathbf{p}_1, \dots, \mathbf{p}_M)^T$ . Furthermore, denote by  $\sqrt{h_{ji}}$  the path gain from transmitter  $j$  to user  $i$ . The received signal at user  $i$  is

$$y_i = \sqrt{h_{ii}\mathbf{p}_i}s_i + \sum_{j \neq i}^M \sqrt{h_{ji}\mathbf{p}_j}s_j + n_i,$$

where  $n_i \in \mathcal{CN}(0, \sigma_e^2)$  is additive noise.

Suppose that there is an eavesdropper (EV), which is also equipped with a single antenna. Denoting by  $\sqrt{h_{ie}}$  the path gain from transmitter  $i$  to the EV, the received signal at the EV is

$$y_e = \sum_{i=1}^M \sqrt{h_{ie}\mathbf{p}_i}s_i + n_e,$$

where  $n_e \in \mathcal{CN}(0, \sigma_e^2)$  is additive noise.

Under the perfect CSI at the transmitters, the information throughput at user  $i$  is

$$f_i(\mathbf{p}) \triangleq \ln \left( 1 + \frac{h_{ii}\mathbf{p}_i}{\sum_{j \neq i}^M h_{ji}\mathbf{p}_j + \sigma_i^2} \right). \quad (1)$$

With the EV considered as part of the legitimate network, the path gain  $\sqrt{h_{ie}}$  can also be assumed known [23]. The wiretapped throughput for user  $i$  at the EV is

$$g_i(\mathbf{p}) \triangleq \ln \left( 1 + \frac{h_{ie}\mathbf{p}_i}{\sum_{j \neq i}^M h_{je}\mathbf{p}_j + \sigma_e^2} \right). \quad (2)$$

The secrecy throughput in transmitting information  $s_i$  to user  $i$  while keeping it confidential from the eavesdropper is defined as

$$\max\{f_i(\mathbf{p}) - g_i(\mathbf{p}), 0\}. \quad (3)$$

We consider the following fundamental optimization problems in a such network: the maximin secrecy throughput optimization

$$\max_{\mathbf{p}} \Phi_{\text{sp}}(\mathbf{p}) \triangleq \min_{i=1, \dots, M} [f_i(\mathbf{p}) - g_i(\mathbf{p})] \quad (4a)$$

$$\text{s.t. } 0 < \mathbf{p}_i \leq P_i, i = 1, \dots, M, \quad (4b)$$

and the network secure energy efficiency (SEE) maximization under users’ secrecy throughput quality-of-service (QoS) requirements

$$\max_{\mathbf{p}} \Phi_{\text{ee}}(\mathbf{p}) \triangleq \frac{\sum_{i=1}^M [f_i(\mathbf{p}) - g_i(\mathbf{p})]}{\zeta \sum_{i=1}^M \mathbf{p}_i + P_c} \quad \text{s.t. } (4b), \quad (5a)$$

$$f_i(\mathbf{p}) - g_i(\mathbf{p}) \geq c_i, i = 1, \dots, M, \quad (5b)$$

or the maximin transmitter EE optimization under users’ secrecy throughput QoS requirements

$$\max_{\mathbf{p}} \min_{i=1, \dots, M} \frac{f_i(\mathbf{p}) - g_i(\mathbf{p})}{\zeta \mathbf{p}_i + P_c^i} \quad \text{s.t. } (4b), (5b). \quad (6)$$

Here  $\zeta$  is the reciprocal of the drain efficiency of the power amplifier,  $P_c^i$  is the circuit power at transmitter  $i$  and  $P_c = \sum_{i=1}^M P_c^i$ . As the numerator in the objective function in (5) is the sum secrecy throughput while the denominator is the network power consumption, the objective function in (5) expresses the network SEE in terms of nats/s/Joule. Similarly, each subfunction in (6) expresses the SEE in for transmitting the information  $s_i$ . Moreover, the constraint (5b) for given thresholds  $c_i$  sets the QoS for the users in terms of the secrecy throughput. This constraint is nonconvex, which is in contrast to the throughput constraint

$$f_i(\mathbf{p}) \geq \tilde{c}_i, i = 1, \dots, M,$$

which is equivalent to the linear constraint

$$h_{ii}\mathbf{p}_i \geq (e^{\tilde{c}_i} - 1) \left( \sum_{j \neq i} h_{ji}\mathbf{p}_j + \sigma_i^2 \right), i = 1, \dots, M.$$

A popular now approach [24] is to treat  $f_i - g_i$  in (4) as a d.c. (difference of two concave functions) function [25]:

$f_i(\mathbf{p}) - g_i(\mathbf{p}) = \tilde{f}_i(\mathbf{p}) - \tilde{g}_i(\mathbf{p})$  with  $\tilde{f}_i(\mathbf{p}) = \ln(\sum_{j=1}^M h_{ji}\mathbf{p}_j + \sigma_i^2) + \ln(\sum_{j \neq i}^M h_{je}\mathbf{p}_j + \sigma_e^2)$  and  $\tilde{g}_i(\mathbf{p}) = \ln(\sum_{j \neq i}^M h_{ji}\mathbf{p}_j + \sigma_i^2) + \ln(\sum_{j=1}^M h_{je}\mathbf{p}_j + \sigma_e^2)$  which are concave. Then at each iteration,  $\tilde{f}_i$  is linearized while  $\tilde{g}_i$  is innerly approximated by a concave quadratic function for a lower approximation of  $\tilde{f}_i - \tilde{g}_i$  [26], [27]. As a result, each iteration invokes solution of a simple convex quadratic optimization problem with the logarithmic function optimization of high computational complexity avoided.

Our next subsections are devoted to efficient computational approach to solving each of (4), (5) and (6) without d.c. representation.

#### A. Max-min secrecy throughput optimization

At every  $p^{(\kappa)} \in R_+^M \triangleq \{(x_1, \dots, x_M)^T : x_k > 0, k = 1, \dots, M\}$ , applying inequality (72) in the Appendix II for  $x = 1/h_{ii}\mathbf{p}_i$ ,  $y = \sum_{j \neq i}^M h_{ji}\mathbf{p}_j + \sigma_i^2$  and  $\bar{x} = 1/h_{ii}p_i^{(\kappa)}$ ,  $\bar{y} = \sum_{j \neq i}^M h_{ji}p_j^{(\kappa)} + \sigma_i^2$  yields

$$f_i(\mathbf{p}) \geq f_i^{(\kappa)}(\mathbf{p}) \quad (7)$$

for

$$f_i^{(\kappa)}(\mathbf{p}) \triangleq \ln(1 + x_i^{(\kappa)}) + \frac{x_i^{(\kappa)}}{1 + x_i^{(\kappa)}} \left( 2 - \frac{p_i^{(\kappa)}}{\mathbf{p}_i} - \frac{\sum_{j \neq i} h_{ji}\mathbf{p}_j + \sigma_i^2}{\sum_{j \neq i}^M h_{ji}p_j^{(\kappa)} + \sigma_i^2} \right). \quad (8)$$

On the other hand, applying inequality (75) in the Appendix II for  $x = h_{ie}\mathbf{p}_i$ ,  $y = \sum_{j \neq i}^M h_{je}\mathbf{p}_j$  and  $\bar{x} = h_{ie}p_i^{(\kappa)}$ ,  $\bar{y} = \sum_{j \neq i}^M h_{je}p_j^{(\kappa)}$  yields

$$g_i(\mathbf{p}) \leq g_i^{(\kappa)}(\mathbf{p}), \quad (9)$$

for

$$g_i^{(\kappa)}(\mathbf{p}) = \ln(1 + x_{e,i}^{(\kappa)}) + \frac{1}{1 + x_{e,i}^{(\kappa)}} \times \left( \frac{0.5h_{ie}(\mathbf{p}_i^2/p_i^{(\kappa)} + p_i^{(\kappa)})}{\sum_{j \neq i}^M h_{je}\mathbf{p}_j + \sigma_e^2} - x_{e,i}^{(\kappa)} \right). \quad (10)$$

Initialized by a feasible  $p^{(0)}$  for the convex constraint (4b), at the  $\kappa$ -th iteration we solve the convex optimization problem

$$\max_{\mathbf{p}} \Phi_{\text{sp}}^{(\kappa)}(\mathbf{p}) \triangleq \min_{i=1, \dots, M} [f_i^{(\kappa)}(\mathbf{p}) - g_i^{(\kappa)}(\mathbf{p})] \quad \text{s.t.} \quad (4b) \quad (11)$$

to generate the next iterative point  $p^{(\kappa+1)}$ . As (11) involves  $M$  decision variables and  $M$  linear constraints, its computational complexity is  $\mathcal{O}(M^2M^{2.5} + M^{3.5})$ .

One can see that  $\Phi_{\text{sp}}(\mathbf{p}) \geq F_{\text{sp}}^{(\kappa)}(\mathbf{p}) \forall \mathbf{p} \in \mathbb{R}_+^M$  and  $\Phi_{\text{sp}}(p^{(\kappa)}) = F_{\text{sp}}^{(\kappa)}(p^{(\kappa)})$ . Furthermore,  $\Phi_{\text{sp}}^{(\kappa)}(p^{(\kappa+1)}) > \Phi_{\text{sp}}^{(\kappa)}(p^{(\kappa)})$  if  $p^{(\kappa+1)} \neq p^{(\kappa)}$  because the former is the optimal solution of (11) while the latter is its feasible point. Therefore,

$$\Phi_{\text{sp}}(p^{(\kappa+1)}) \geq \Phi_{\text{sp}}^{(\kappa)}(p^{(\kappa+1)}) > \Phi_{\text{sp}}^{(\kappa)}(p^{(\kappa)}) = \Phi_{\text{sp}}(p^{(\kappa)}), \quad (12)$$

i.e.  $p^{(\kappa+1)}$  is better than  $p^{(\kappa)}$ ; as such  $\{p^{(\kappa)}\}$  is a sequence of improved points that converges at least to a locally optimal solution of (4) satisfying the first order necessary optimality

condition [28, Prop. 1]. In summary, we propose in Algorithm 1 a path-following computational procedure for the maximin secrecy throughput optimization problem (4).

---

**Algorithm 1** Path-following algorithm for maximin secrecy throughput optimization

---

**Initialization:** Set  $\kappa = 0$ . Choose an initial feasible point  $p^{(0)}$  for the convex constraints (4b). Calculate  $R_{\min}^{(0)}$  as the value of the objective in (4) at  $p^{(0)}$ .

**repeat**

- Set  $\kappa = \kappa + 1$ .
- Solve the convex optimization problem (11) to obtain the solution  $p^{(\kappa)}$ .
- Calculate  $R_{\min}^{(\kappa)}$  as the value of the objective in (4) at  $p^{(\kappa)}$ .

**until**  $\frac{R_{\min}^{(\kappa)} - R_{\min}^{(\kappa-1)}}{R_{\min}^{(\kappa-1)}} \leq \epsilon_{\text{tol}}$ .

---

#### B. Secure energy efficient maximization

Define

$$\pi(\mathbf{p}) = \zeta \sum_{i=1}^M \mathbf{p}_i + P_c.$$

Applying the inequality (73) in Appendix II for  $x = 1/h_{ii}\mathbf{p}_i$ ,  $y = \sum_{j \neq i}^M h_{ji}\mathbf{p}_j + \sigma_i^2$ ,  $t = \pi(\mathbf{p})$ , and  $\bar{x} = 1/h_{ii}p_i^{(\kappa)}$ ,  $\bar{y} = \sum_{j \neq i}^M h_{ji}p_j^{(\kappa)} + \sigma_i^2$ ,  $\bar{t} = \pi(p^{(\kappa)})$  yields

$$\frac{f_i(\mathbf{p})}{\pi(\mathbf{p})} \geq F_i^{(\kappa)}(\mathbf{p}) \quad (13)$$

for

$$F_i^{(\kappa)}(\mathbf{p}) \triangleq \frac{2 \ln(1 + x_i^{(\kappa)})}{\pi(p^{(\kappa)})} + \frac{x_i^{(\kappa)}}{\pi(p^{(\kappa)})(1 + x_i^{(\kappa)})} \times \left( 2 - \frac{p_i^{(\kappa)}}{\mathbf{p}_i} - \frac{\sum_{j \neq i} h_{ji}\mathbf{p}_j + \sigma_i^2}{\sum_{j \neq i}^M h_{ji}p_j^{(\kappa)} + \sigma_i^2} \right) - \frac{\ln(1 + x_i^{(\kappa)})}{\pi^2(p^{(\kappa)})} \pi(\mathbf{p}). \quad (14)$$

On the other hand, applying inequality (75) in Appendix II for  $\alpha = 1 + \ln(2)$ ,  $x = h_{ie}\mathbf{p}_i / (\sum_{j \neq i} h_{je}\mathbf{p}_j + \sigma_e^2)$ ,  $t = \pi(\mathbf{p})$  and  $\bar{x} \triangleq h_{ie}p_i^{(\kappa)} / (\sum_{j \neq i} h_{je}p_j^{(\kappa)} + \sigma_e^2)$ ,  $\bar{t} = \pi(p^{(\kappa)})$  yields

$$\frac{-g_i(\mathbf{p})}{\pi(\mathbf{p})} \geq 2 \frac{\alpha - \ln(1 + x_{e,i}^{(\kappa)})}{\pi(p^{(\kappa)})} + \frac{x_{e,i}^{(\kappa)}}{(1 + x_{e,i}^{(\kappa)})\pi(p^{(\kappa)})} - \frac{1}{(1 + x_{e,i}^{(\kappa)})\pi(p^{(\kappa)})} \frac{h_{ie}\mathbf{p}_i}{\sum_{j \neq i} h_{je}\mathbf{p}_j + \sigma_e^2} - \frac{\alpha - \ln(1 + x_{e,i}^{(\kappa)})}{\pi^2(p^{(\kappa)})} \pi(\mathbf{p}) - \frac{\alpha}{\pi(\mathbf{p})}, \quad (15)$$

which together with (76) in Appendix II yield

$$\frac{f_i(\mathbf{p}) - g_i(\mathbf{p})}{\pi(\mathbf{p})} \geq G_i^{(\kappa)}(\mathbf{p}) \quad (16)$$

for the concave function

$$G_i^{(\kappa)}(\mathbf{p}) \triangleq 2 \frac{\alpha - \ln(1 + x_{e,i}^{(\kappa)})}{\pi(p^{(\kappa)})} + \frac{x_{e,i}^{(\kappa)}}{(1 + x_{e,i}^{(\kappa)})\pi(p^{(\kappa)})} - \frac{1}{(1 + x_{e,i}^{(\kappa)})\pi(p^{(\kappa)})} \frac{0.5h_{ie}(\mathbf{p}_i^2/p_i^{(\kappa)} + p_i^{(\kappa)})}{\sum_{j \neq i} h_{je}\mathbf{p}_j + \sigma_e^2} - \frac{\alpha - \ln(1 + x_{e,i}^{(\kappa)})}{\pi^2(p^{(\kappa)})}\pi(\mathbf{p}) - \frac{\alpha}{\pi(\mathbf{p})}. \quad (17)$$

Initialized by a feasible point  $p^{(0)}$  for (5), we solve the following convex optimization problem at the  $\kappa$ -th iteration to generate the next iterative point  $p^{(\kappa+1)}$ :

$$\max_{\mathbf{p}} \Phi_{ee}^{(\kappa)}(\mathbf{p}) \triangleq \sum_{i=1}^M [F_i^{(\kappa)}(\mathbf{p}) + G_i^{(\kappa)}(\mathbf{p})] \quad \text{s.t.} \quad (4b), \quad (18a)$$

$$f_i^{(\kappa)}(\mathbf{p}) - g_i^{(\kappa)}(\mathbf{p}) \geq c_i, i = 1, \dots, M. \quad (18b)$$

The computational complexity of (18) is  $\mathcal{O}(M^2(2M)^{2.5} + (2M)^{3.5})$ .

Due to (7) and (9), the nonconvex constraint (5b) in (5) is implied by the convex constraint (18b) in (18). Similarly to (12), we can show that  $\Phi_{ee}(p^{(\kappa+1)}) > \Phi_{ee}(p^{(\kappa)})$  whenever  $p^{(\kappa+1)} \neq p^{(\kappa)}$ ; as such the computational procedure that invokes the convex program (18) to generate the next iterative point, is path-following for (5), which at least converges to its locally optimal solution satisfying the Karush-Kuh-Tucker (KKT) conditions of optimality.

Recalling the definition (9) and (10) of functions  $f_i^{(\kappa)}$  and  $g_i^{(\kappa)}$ , initialized by any feasible point  $\tilde{p}^{(0)}$  for the convex constraint (4b), we generate  $\tilde{p}^{(\kappa+1)}$ ,  $\kappa = 0, \dots$ , as the optimal solution of the convex optimization problem

$$\max_{\mathbf{p}} \min_{i=1, \dots, M} \frac{f_i^{(\kappa)}(\mathbf{p}) - g_i^{(\kappa)}(\mathbf{p})}{c_i} \quad \text{s.t.} \quad (4b) \quad (19)$$

until  $\tilde{p}^{(\kappa+1)}$  such that  $\min_{i=1, \dots, M} (f_i(p^{(\kappa+1)}) - g_i(p^{(\kappa+1)}))/c_i \geq 1$  is found and thus  $p^{(0)} = \tilde{p}^{(\kappa+1)}$  is feasible for (5) that is needed for the initial step.

Analogously, to address the maximin secure energy efficient optimization problem (6) define

$$\pi_i(\mathbf{p}_i) = \zeta \mathbf{p}_i + P_c^i.$$

Similarly to (13) and (16) the following inequalities can be obtained:

$$\frac{f_i(\mathbf{p})}{\pi_i(\mathbf{p}_i)} \geq \tilde{F}_i^{(\kappa)}(\mathbf{p}_i) \quad (20)$$

$$\frac{-g_i(\mathbf{p})}{\pi_i(\mathbf{p}_i)} \geq \tilde{G}_i^{(\kappa)}(\mathbf{p}_i) \quad (21)$$

for

$$\tilde{F}_i^{(\kappa)}(\mathbf{p}_i) \triangleq \frac{2 \ln(1 + x_i^{(\kappa)})}{\pi_i(p_i^{(\kappa)})} + \frac{x_i^{(\kappa)}}{\pi_i(p_i^{(\kappa)})(1 + x_i^{(\kappa)})} \times \left( 2 - \frac{p_i^{(\kappa)}}{\mathbf{p}_i} - \frac{\sum_{j \neq i} h_{ji}\mathbf{p}_j + \sigma_e^2}{\sum_{j \neq i} h_{ji}p_j^{(\kappa)} + \sigma_e^2} \right) - \frac{\ln(1 + x_i^{(\kappa)})}{\pi_i^2(p_i^{(\kappa)})}\pi_i(\mathbf{p}_i) \quad (22)$$

$$\tilde{G}_i^{(\kappa)}(\mathbf{p}_i) \triangleq 2 \frac{\alpha - \ln(1 + x_{e,i}^{(\kappa)})}{\pi_i(p_i^{(\kappa)})} + \frac{x_{e,i}^{(\kappa)}}{(1 + x_{e,i}^{(\kappa)})\pi_i(p_i^{(\kappa)})} - \frac{1}{(1 + x_{e,i}^{(\kappa)})\pi_i(p_i^{(\kappa)})} \frac{0.5h_{ie}(\mathbf{p}_i^2/p_i^{(\kappa)} + p_i^{(\kappa)})}{\sum_{j \neq i} h_{je}\mathbf{p}_j + \sigma_e^2} - \frac{\alpha - \ln(1 + x_{e,i}^{(\kappa)})}{\pi_i^2(p_i^{(\kappa)})}\pi_i(\mathbf{p}_i) - \frac{\alpha}{\pi_i(\mathbf{p}_i)}. \quad (23)$$

Initialized a feasible point  $p^{(0)}$  for (6), which is found by using the generation (19), the following convex optimization problem at the  $\kappa$ -th iteration is proposed to generate the next iterative point  $p^{(\kappa+1)}$ :

$$\max_{\mathbf{p}} \min_{i=1, \dots, M} [\tilde{F}_i^{(\kappa)}(\mathbf{p}) + \tilde{G}_i^{(\kappa)}(\mathbf{p})] \quad \text{s.t.} \quad (4b), f_i^{(\kappa)}(\mathbf{p}) - g_i^{(\kappa)}(\mathbf{p}) \geq c_i, i = 1, \dots, M. \quad (24)$$

The computational complexity of (24) is similar to that of (18).

The computational procedure that invokes the convex program (24) to generate the next iterative point, is path-following for (6), which at least converges to its locally optimal solution satisfying the first order necessary optimality condition.

### III. INTERFERENCE NETWORKS UNDER PARTIAL WIRETAP CSI

When the EV is not part of the legitimate network, it is almost impossible to estimate channels  $h_{ie}$  from the transmitters to it. It is common to assume that  $h_{ie} = \bar{h}_{ie}\chi_{ie}$ , where  $\chi_{ie}$  is an exponential distribution with the unit mean and  $\bar{h}_{ie}$  is a known deterministic quantity. Accordingly, instead of (2), the wiretapped throughput for user  $i$  at the EV is defined via the following throughput outage [29]–[33]:

$$g_{i,o}(\mathbf{p}) \triangleq \max \{ \ln(1 + \mathbf{r}_i) : \text{Prob} \left( \frac{h_{ie}\mathbf{p}_i}{\sum_{j \neq i} h_{je}\mathbf{p}_j + \sigma_e^2} < \mathbf{r}_i \right) \leq \epsilon_{EV} \} \quad (25)$$

for  $\epsilon_{EV} > 0$ . Using (63) in Appendix I, it follows that

$$g_{i,o}(\mathbf{p}) = \ln(1 + \mathbf{r}_i)$$

where

$$\mathbf{p}_i \bar{h}_{ie} \ln(1 - \epsilon_{EV}) + \mathbf{r}_i \sigma_e^2 \mathbf{p}_i + \bar{h}_{ie} \sum_{j \neq i}^M \ln \left( 1 + \frac{\mathbf{r}_i \bar{h}_{je} \mathbf{p}_j}{\bar{h}_{ie} \mathbf{p}_i} \right) = 0, \quad i = 1, \dots, M. \quad (26)$$

Therefore, the problem of maximin secrecy throughput optimization can be formulated as

$$\max_{\mathbf{p}, \mathbf{r}} \min_{i=1, \dots, M} [f_i(\mathbf{p}) - \ln(1 + \mathbf{r}_i)] \quad \text{s.t.} \quad (4b), (26), \quad (27a)$$

$$\mathbf{r}_i > 0, i = 1, \dots, M. \quad (27b)$$

The following result unravels the computationally intractable nonlinear equality constraints in (26).

*Proposition 1:* The problem (27) is equivalent to the following problem

$$\max_{\mathbf{p}, \mathbf{r}} \min_{i=1, \dots, M} [f_i(\mathbf{p}) - \ln(1 + \mathbf{r}_i)] \quad \text{s.t.} \quad (4b), (27b), \quad (28a)$$

$$\mathbf{p}_i \bar{h}_{ie} \ln(1 - \epsilon_{EV}) + \mathbf{r}_i \sigma_e^2 + \mathbf{p}_i \bar{h}_{ie} \times \sum_{j \neq i}^M \ln \left( 1 + \frac{\mathbf{r}_i \bar{h}_{je} \mathbf{p}_j}{\bar{h}_{ie} \mathbf{p}_i} \right) \geq 0, \quad i = 1, \dots, M. \quad (28b)$$

*Proof:* Since the equality constraint (26) implies the inequality constraint (28b), it is true that

the optimal value of (27)  $\leq$  the optimal value of (28).

We now show that there is an optimal solution of (28) satisfies the equality constraint (26) and thus

the optimal value of (28)  $\leq$  the optimal value of (27),

showing the equivalence between (28) and (27). Indeed, suppose that at the optimality,

$$\mathbf{p}_i \bar{h}_{ie} \ln(1 - \epsilon_{EV}) + \mathbf{r}_i \sigma_e^2 + \mathbf{p}_i \bar{h}_{ie} \sum_{j \neq i}^M \ln \left( 1 + \frac{\mathbf{r}_i \bar{h}_{je} \mathbf{p}_j}{\bar{h}_{ie} \mathbf{p}_i} \right) > 0$$

for some  $i = 1, \dots, M$ . Then there is  $0 < \gamma_i < 1$  such that

$$\mathbf{p}_i \bar{h}_{ie} \ln(1 - \epsilon_{EV}) + (\gamma_i \mathbf{r}_i) \sigma_e^2 + \mathbf{p}_i \bar{h}_{ie} \times \sum_{j \neq i}^M \ln \left( 1 + \frac{\gamma_i \bar{h}_{je} \mathbf{p}_j}{\bar{h}_{ie} \mathbf{p}_i} \right) = 0,$$

that yields

$$f_i(\mathbf{p}) - \ln(1 + \gamma_i \mathbf{r}_i) > f_i(\mathbf{p}) - \ln(1 + \mathbf{r}_i),$$

so  $\gamma_i \mathbf{r}_i$  is also the optimal solution of (28), which satisfies the equality constraint (26).  $\square$

To address problem (28), note that a lower bounding function for the first term in (28a) is  $f_i^{(\kappa)}(\mathbf{p})$  defined by (8), while an upper bounding function for the second term in (28a) is the following linear function

$$a_i^{(\kappa)}(\mathbf{r}_i) = \ln(1 + r_i^{(\kappa)}) - \frac{r_i^{(\kappa)}}{r_i^{(\kappa)} + 1} + \frac{\mathbf{r}_i}{r_i^{(\kappa)} + 1}. \quad (29)$$

The main difficulty now is to develop a lower bounding approximation for the function in the left hand side (LHS) of constraint (28b). Applying inequality (72) in Appendix II for  $x = 1/\mathbf{r}_i \bar{h}_{je} \mathbf{p}_j$ ,  $y = \bar{h}_{ie} \mathbf{p}_i$  and  $\bar{x} = 1/r_i^{(\kappa)} \bar{h}_{je} p_j^{(\kappa)}$ ,  $\bar{y} = \bar{h}_{ie} p_i^{(\kappa)}$  yields

$$\ln \left( 1 + \frac{\mathbf{r}_i \bar{h}_{je} \mathbf{p}_j}{\bar{h}_{ie} \mathbf{p}_i} \right) \geq \lambda_{ij}^{(\kappa)}(\mathbf{r}_i, \mathbf{p}_j, \mathbf{p}_i) \quad (30)$$

for

$$\lambda_{ij}^{(\kappa)}(\mathbf{r}_i, \mathbf{p}_j, \mathbf{p}_i) \triangleq \ln(1 + x_{ij}^{(\kappa)}) + y_{ij}^{(\kappa)} \times \left( 2 - \frac{r_i^{(\kappa)} p_j^{(\kappa)}}{\mathbf{r}_i \mathbf{p}_j} - \frac{\mathbf{p}_i}{p_i^{(\kappa)}} \right) \quad (31)$$

with  $x_{ij}^{(\kappa)} \triangleq r_i^{(\kappa)} \bar{h}_{je} p_j^{(\kappa)} / \bar{h}_{ie} p_i^{(\kappa)}$  and  $y_{ij}^{(\kappa)} \triangleq x_{ij}^{(\kappa)} / (x_{ij}^{(\kappa)} + 1)$ . Therefore, over the trust region

$$\lambda_{ij}^{(\kappa)}(\mathbf{r}_i, \mathbf{p}_j, \mathbf{p}_i) \geq 0, \quad 2.5 - \frac{\mathbf{r}_i}{r_i^{(\kappa)}} - \frac{\mathbf{p}_j}{p_j^{(\kappa)}} \geq 0 \quad (32)$$

it is true that

$$\begin{aligned} & \mathbf{p}_i \ln(1 + \frac{\mathbf{r}_i \bar{h}_{je} \mathbf{p}_j}{\bar{h}_{ie} \mathbf{p}_i}) \geq \\ & \mathbf{p}_i \ln(1 + x_{ij}^{(\kappa)}) + y_{ij}^{(\kappa)} \left( 2\mathbf{p}_i - \frac{r_i^{(\kappa)} p_j^{(\kappa)} \mathbf{p}_i}{\mathbf{r}_i \mathbf{p}_j} - \frac{\mathbf{p}_i^2}{p_i^{(\kappa)}} \right) = \\ & \left( \ln(1 + x_{ij}^{(\kappa)}) + 2y_{ij}^{(\kappa)} \right) \mathbf{p}_i - 0.5y_{ij}^{(\kappa)} \left[ 2 \frac{\mathbf{p}_i^2}{p_i^{(\kappa)}} \right. \\ & \quad \left. + \left( \frac{\sqrt{2\mathbf{p}_i}}{\sqrt{p_i^{(\kappa)}}} + \frac{\sqrt{p_i^{(\kappa)}} r_i^{(\kappa)} p_j^{(\kappa)}}{\sqrt{2\mathbf{r}_i \mathbf{p}_j}} \right)^2 - \frac{2\mathbf{p}_i^2}{p_i^{(\kappa)}} \right. \\ & \quad \left. - \frac{p_i^{(\kappa)} (r_i^{(\kappa)} p_j^{(\kappa)})^2}{2\mathbf{r}_i^2 \mathbf{p}_j^2} \right] \geq \\ & \Lambda_i^{(\kappa)}(\mathbf{r}_i, \mathbf{p}_j, \mathbf{p}_i) \quad (33) \end{aligned}$$

for

$$\begin{aligned} \Lambda_i^{(\kappa)}(\mathbf{r}_i, \mathbf{p}_j, \mathbf{p}_i) &= \left( \ln(1 + x_{ij}^{(\kappa)}) + 2y_{ij}^{(\kappa)} \right) \mathbf{p}_i \\ &\quad - 0.5y_{ij}^{(\kappa)} \left( \frac{\sqrt{2\mathbf{p}_i}}{\sqrt{p_i^{(\kappa)}}} + \frac{\sqrt{p_i^{(\kappa)}} r_i^{(\kappa)} p_j^{(\kappa)}}{\sqrt{2\mathbf{r}_i \mathbf{p}_j}} \right)^2 \\ &\quad - 0.5y_{ij}^{(\kappa)} p_i^{(\kappa)} \left( \frac{\mathbf{r}_i}{r_i^{(\kappa)}} + \frac{\mathbf{p}_j}{p_j^{(\kappa)}} - 2.5 \right). \end{aligned}$$

Note that in obtaining (33) we also used the fact that function  $\nu(\mathbf{r}_i, \mathbf{p}_j) \triangleq 1/\mathbf{r}_i^2 \mathbf{p}_j^2$  is convex in the domain  $\{\mathbf{r}_i > 0, \mathbf{p}_j > 0\}$  and accordingly [25]  $1/\mathbf{r}_i^2 \mathbf{p}_j^2 \geq \nu(r_i^{(\kappa)}, p_j^{(\kappa)}) + \langle \nabla \nu(r_i^{(\kappa)}, p_j^{(\kappa)}), (\mathbf{r}_i, \mathbf{p}_j) - (r_i^{(\kappa)}, p_j^{(\kappa)}) \rangle = [5 - 2(\mathbf{r}_i/r_i^{(\kappa)} + \mathbf{p}_j/p_j^{(\kappa)})]/(r_i^{(\kappa)} p_j^{(\kappa)})^2$ .

Initialized from a feasible point  $(p^{(0)}, r^{(0)})$  for (28) we solve the following convex program at the  $\kappa$ -th iteration to generate  $(p^{(\kappa+1)}, r_u^{(\kappa+1)})$ :

$$\max_{\mathbf{p}, \mathbf{r}} \min_{i=1, \dots, M} [f_i^{(\kappa)}(\mathbf{p}) - a_i^{(\kappa)}(\mathbf{r}_i)] \quad \text{s.t.} \quad (4b), (27b), (32), (34a)$$

$$\mathbf{p}_i \bar{h}_{ie} \ln(1 - \epsilon_{EV}) + \sigma_e^2 \mathbf{r}_i + \bar{h}_{ie} \sum_{j \neq i}^M \Lambda_{ij}^{(\kappa)}(\mathbf{r}_i, \mathbf{p}_j, \mathbf{p}_i) \geq 0, \quad (34b)$$

$$i = 1, \dots, M.$$

The computational complexity of (34) is  $\mathcal{O}((2M)^2(5M)^{2.5} + (5M)^{2.5})$  because it involves  $2M$  decision variables and  $5M$  linear and quadratic constraints.

Then  $r_i^{(\kappa+1)}$  is found from solving

$$0 = \psi_i(\mathbf{r}_i) \triangleq p_i^{(\kappa+1)} \bar{h}_{ie} \ln(1 - \epsilon_{EV}) + \mathbf{r}_i \sigma_e^2 + p_i^{(\kappa+1)} \bar{h}_{ie} \sum_{j \neq i}^M \ln \left( 1 + \frac{\mathbf{r}_i \bar{h}_{je} p_j^{(\kappa+1)}}{\bar{h}_{ie} p_i^{(\kappa+1)}} \right), \quad (35)$$

$$i = 1, \dots, M,$$

by bisection on  $[0, r_{u,i}^{(\kappa+1)}]$  such that

$$0 \leq \psi_i(r_i^{(\kappa+1)}) \leq \epsilon_b \quad (\text{tolerance}). \quad (36)$$

A bisection on  $[r_l, r_u]$  for solving  $\psi_i(\mathbf{r}_i) = 0$  where  $\psi_i$  increases in  $\mathbf{r}_i > 0$  is implemented as follows:

- Define  $r_i = (r_l + r_u)/2$ . Reset  $r_l = r_i$  if  $\psi_i(r_i) < 0$ . Otherwise reset  $r_u = r_i$ .
- Terminate until  $0 \leq \psi_i(r_i) \leq \epsilon_b$ .

In summary, we propose in Algorithm 2 a path-following computational procedure for the maximin secrecy throughput optimization problem (28), which at least converges to its locally optimal solution satisfying the first order necessary optimality condition.

**Algorithm 2** Path-following algorithm for maximin secrecy throughput optimization

**Initialization:** Set  $\kappa = 0$ . Choose an initial feasible point  $(p^{(0)}, r^{(0)})$  for (28) and calculate  $R_{\min}^{(0)}$  as the value of the objective function in (28) at  $(p^{(0)}, r^{(0)})$ .

**repeat**

- Set  $\kappa = \kappa + 1$ .
- Solve the convex optimization problem (34) to obtain the solution  $(p^{(\kappa)}, r_u^{(\kappa)})$ .
- Solve the nonlinear equations (35) to obtain the roots  $r_i^{(\kappa)}$ .
- Calculate  $R_{\min}^{(\kappa)}$  as the value of the objective function in (28) at  $(p^{(\kappa)}, r^{(\kappa)})$ .

**until**  $\frac{R_{\min}^{(\kappa)} - R_{\min}^{(\kappa-1)}}{R_{\min}^{(\kappa-1)}} \leq \epsilon_{\text{tol}}$ .

A feasible  $(p^{(0)}, r^{(0)})$  is found as follows: taking  $p^{(0)}$  feasible to the power constraint (4b) and finding  $r^{(0)}$  from solving

$$0 = \psi_i(\mathbf{r}_i) \triangleq p_i^{(0)} \bar{h}_{ie} \ln(1 - \epsilon_{EV}) + \mathbf{r}_i \sigma_e^2 + \bar{h}_{ie} p_i^{(0)} \sum_{j \neq i}^M \ln \left( 1 + \frac{\mathbf{r}_i \bar{h}_{je} p_j^{(0)}}{\bar{h}_{ie} p_i^{(0)}} \right)$$

$$i = 1, \dots, M,$$

by bisection on  $[0, r_{u,i}^{(0)}]$  with  $\psi_i(r_{u,i}^{(0)}) > 0$ . Such  $r_{u,i}^{(0)}$  can be easily found: from any  $r_{u,i} > 0$ , if  $\psi_i(r_{u,i}) \geq 0$  then we are done. Otherwise reset  $r_{u,i} \leftarrow 2r_{u,i}$  and check  $\psi_i(r_{u,i})$ . Stop when  $\psi(r_{u,i}) > 0$ . Intuitively, taking  $r_{u,i}^{(0)} = \bar{h}_{ie} p_i^{(0)} / \sigma_e^2$  will work.

Furthermore, the problem of SEE maximization can be formulated as

$$\max_{\mathbf{p}, \mathbf{r}} \frac{\sum_{i=1}^M (f_i(\mathbf{p}) - \ln(1 + \mathbf{r}_i))}{\pi(\mathbf{p})} \quad \text{s.t. (4b), (27b), (28b)} \quad (37a)$$

$$f_i(\mathbf{p}) - \ln(1 + \mathbf{r}_i) \geq c_i, i = 1, \dots, M. \quad (37b)$$

Using the inequality (74) in Appendix II leads to

$$\frac{-\ln(1 + \mathbf{r}_i)}{\pi(\mathbf{p})} \geq \tilde{a}_i^{(\kappa)}(\mathbf{r}_i, \mathbf{p})$$

for

$$\tilde{a}_i^{(\kappa)}(\mathbf{r}_i, \mathbf{p}) \triangleq 2 \frac{\alpha - \ln(1 + r_i^{(\kappa)})}{\pi(p^{(\kappa)})} + \frac{r_i^{(\kappa)}}{\pi(p^{(\kappa)})(1 + r_i^{(\kappa)})} - \frac{\mathbf{r}_i}{\pi(p^{(\kappa)})(1 + r_i^{(\kappa)})} - \frac{\alpha - \ln(1 + r_i^{(\kappa)})}{\pi^2(p^{(\kappa)})} \pi(\mathbf{p}) - \frac{\alpha}{\pi(\mathbf{p})}. \quad (38)$$

Initialized by a feasible  $(p^{(0)}, r^{(0)})$ , the following convex program is solved to generate  $(p^{(\kappa+1)}, r^{(\kappa+1)})$  at the  $\kappa$  iteration:

$$\max_{\mathbf{p}, \mathbf{r}} \sum_{i=1}^M [F_i^{(\kappa)}(\mathbf{p}) + \tilde{a}_i^{(\kappa)}(\mathbf{r}_i, \mathbf{p})] \quad (39a)$$

$$\text{s.t.} \quad (4b), (27b), (32), (34b), \quad (39b)$$

$$f_i^{(\kappa)}(\mathbf{p}) - a_i^{(\kappa)}(\mathbf{r}_i) \geq c_i, i = 1, \dots, M. \quad (39c)$$

The computational complexity of (34) is  $\mathcal{O}((2M)^2(6M)^{2.5} + (6M)^{2.5})$ .

It can be shown that the computational procedure that invokes the convex program (39) to generate the next iterative point, is path-following for (37), which at least converges to its locally optimal solution satisfying the KKT conditions. A point  $(p^{(0)}, r^{(0)})$  is feasible for (37) if and only if  $\min_{i=1, \dots, M} [f_i(p^{(0)}) - \ln(1 + r_i^{(0)})] / c_i \geq 1$  and thus can be easily located by adapting Algorithm 2.

Similarly, a path-following procedure for the following maximin SEE optimization problem can be proposed

$$\max_{\mathbf{p}, \mathbf{r}} \min_{i=1, \dots, M} \frac{f_i(\mathbf{p}) - \ln(1 + \mathbf{r}_i)}{\pi_i(\mathbf{p})} \quad (40a)$$

$$\text{s.t.} \quad (4b), (27b), (28b), (37b). \quad (40b)$$

#### IV. ROBUST OPTIMIZATION

Beside assuming that  $h_{ie} = \bar{h}_{ie} \chi_{ie}$  with an exponential distribution  $\chi_{ie}$  with the unit mean and deterministic  $\bar{h}_{ie}$ , we also assume that CSI of  $h_{ji}$  is not known perfectly in the form  $h_{ji} = \bar{h}_{ji}(1 + \delta \chi_{ji})$  with deterministic  $\bar{h}_{ji}$  and  $\delta$ , and random  $\chi_{ji}$ , which is an independent exponential distribution of the unit mean. Instead of (1), the throughput at user  $i$  is defined via the following outage probability

$$f_{i,o}(\mathbf{p}) \triangleq \max\{\ln(1 + \mathbf{R}_i) : \text{Prob} \left( \frac{h_{ii} \mathbf{p}_i}{\sum_{j \neq i}^M h_{ji} \mathbf{p}_j + \sigma_i^2} < \mathbf{R}_i \right) \leq \epsilon_c\} \quad (41)$$

for  $0 < \epsilon_c \ll 1$ .

Using (67) in Appendix II, it follows that

$$f_{i,o}(\mathbf{p}) = \ln(1 + \mathbf{R}_i), i = 1, \dots, M, \quad (42)$$

where

$$\begin{aligned} & \mathbf{p}_i \bar{h}_{ii} [\delta \ln(1 - \epsilon_c) - 1] + \mathbf{R}_i (\sigma_i^2 + \sum_{j \neq i} \bar{h}_{ji} \mathbf{p}_j) \\ & + \delta \bar{h}_{ii} \mathbf{p}_i \sum_{j \neq i}^M \ln \left( 1 + \frac{\bar{h}_{ji} \mathbf{R}_i \mathbf{p}_j}{\bar{h}_{ii} \mathbf{p}_i} \right) = 0, \quad i = 1, \dots, M. \end{aligned} \quad (43)$$

Therefore, the problem of maximin secrecy throughput robust optimization is defined by

$$\max_{\mathbf{p}, \mathbf{R}, \mathbf{r}} \min_{i=1, \dots, M} [\ln(1 + \mathbf{R}_i) - \ln(1 + \mathbf{r}_i)] \quad (44a)$$

$$\text{s.t.} \quad (4b), (27b), (28b), (43), \quad (44b)$$

$$\mathbf{R}_i > 0, \quad i = 1, \dots, M. \quad (44c)$$

The following result unravels the computationally intractable nonlinear equality constraints in (43):

*Proposition 2:* Problem (44) is equivalent to the following problem

$$\max_{\mathbf{p}, \mathbf{R}, \mathbf{r}} \min_{i=1, \dots, M} [\ln(1 + \mathbf{R}_i) - \ln(1 + \mathbf{r}_i)] \quad (45a)$$

$$\text{s.t.} \quad (4b), (28b), (27b), (44c) \quad (45b)$$

$$\begin{aligned} & \mathbf{p}_i \bar{h}_{ii} [\delta \ln(1 - \epsilon_c) - 1] + \mathbf{R}_i (\sigma_i^2 + \sum_{j \neq i} \bar{h}_{ji} \mathbf{p}_j) \\ & + \delta \bar{h}_{ii} \mathbf{p}_i \sum_{j \neq i}^M \ln \left( 1 + \frac{\bar{h}_{ji} \mathbf{R}_i \mathbf{p}_j}{\bar{h}_{ii} \mathbf{p}_i} \right) \leq 0, \quad (45c) \\ & i = 1, \dots, M. \end{aligned}$$

*Proof:* Again, it is obvious that the optimal value of (44) is not more than the optimal value of (45). Furthermore, at an optimal solution of (45), if

$$\begin{aligned} & \mathbf{p}_i \bar{h}_{ii} [\delta \ln(1 - \epsilon_c) - 1] + \mathbf{R}_i (\sigma_i^2 + \sum_{j \neq i} \bar{h}_{ji} \mathbf{p}_j) \\ & + \delta \bar{h}_{ii} \mathbf{p}_i \sum_{j \neq i}^M \ln \left( 1 + \frac{\bar{h}_{ji} \mathbf{R}_i \mathbf{p}_j}{\bar{h}_{ii} \mathbf{p}_i} \right) < 0, \end{aligned}$$

for some  $i$  then there is  $\gamma > 1$  such that

$$\begin{aligned} & \mathbf{p}_i \bar{h}_{ii} [\delta \ln(1 - \epsilon_c) - 1] + (\gamma \mathbf{R}_i) (\sigma_i^2 + \sum_{j \neq i} \bar{h}_{ji} \mathbf{p}_j) \\ & + \delta \bar{h}_{ii} \mathbf{p}_i \sum_{j \neq i}^M \ln \left( 1 + \frac{\bar{h}_{ji} (\gamma \mathbf{R}_i) \mathbf{p}_j}{\bar{h}_{ii} \mathbf{p}_i} \right) = 0, \end{aligned}$$

which results in  $\ln(1 + \gamma \mathbf{R}_i) > \ln(1 + \mathbf{R}_i)$ , implying that  $\gamma \mathbf{R}_i$  is also an optimal solution of (45). We thus have proved that there is always an optimal solution of (45) to satisfy the equality constraints in (43), so the optimal value of (45) is not more than the optimal value of (44), completing the proof of Proposition 2.  $\square$

To address problem (45), firstly we provide a lower bounding approximation for the first term in the objective function in (45b) as follows

$$\begin{aligned} \ln(1 + \mathbf{R}_i) & \geq A_i^{(\kappa)}(\mathbf{R}_i) \\ & \triangleq \ln(1 + R_i^{(\kappa)}) + \frac{R_i^{(\kappa)}}{R_i^{(\kappa)} + 1} - \frac{(R_i^{(\kappa)})^2}{R_i^{(\kappa)} + 1} \frac{1}{\mathbf{R}_i}. \end{aligned}$$

Next, to obtain an upper bounding approximation for the function in the left hand side of (45c) and thus to provide an inner approximation for constraint (45c), we use the following inequality

$$\begin{aligned} \mathbf{R}_i \mathbf{p}_j & = 0.5(\mathbf{R}_i + \mathbf{p}_j)^2 - 0.5\mathbf{R}_i^2 - 0.5\mathbf{p}_j^2 \\ & \leq \Upsilon_{ij}^{(\kappa)}(\mathbf{R}_i, \mathbf{p}_j) \\ & \triangleq 0.5(\mathbf{R}_i + \mathbf{p}_j)^2 - R_i^{(\kappa)} \mathbf{R}_i + 0.5(R_i^{(\kappa)})^2 \\ & \quad - p_j^{(\kappa)} \mathbf{p}_j + 0.5(p_j^{(\kappa)})^2, \end{aligned} \quad (46)$$

over the trust region

$$2\mathbf{R}_i \geq R_i^{(\kappa)}, 2\mathbf{p}_j \geq p_j^{(\kappa)}. \quad (47)$$

Then

$$\begin{aligned} & \mathbf{p}_i \ln \left( 1 + \frac{\bar{h}_{ji} \mathbf{R}_i \mathbf{p}_j}{\bar{h}_{ii} \mathbf{p}_i} \right) \leq \\ & \mathbf{p}_i \left[ \ln \left( 1 + \frac{\bar{h}_{ji} R_i^{(\kappa)} p_j^{(\kappa)}}{\bar{h}_{ii} p_i^{(\kappa)}} \right) \right. \\ & \quad \left. + \frac{1}{\frac{\bar{h}_{ii}}{\bar{h}_{ji}} + \frac{R_i^{(\kappa)} p_j^{(\kappa)}}{p_i^{(\kappa)}}} \left( \frac{\mathbf{R}_i \mathbf{p}_j}{\mathbf{p}_i} - \frac{R_i^{(\kappa)} p_j^{(\kappa)}}{p_i^{(\kappa)}} \right) \right] \leq \\ & \quad \Phi_{ij}^{(\kappa)}(\mathbf{R}_i, \mathbf{p}_j, \mathbf{p}_i) \triangleq \\ & \quad \mathbf{p}_i \ln \left( 1 + \frac{\bar{h}_{ji} R_i^{(\kappa)} p_j^{(\kappa)}}{\bar{h}_{ii} p_i^{(\kappa)}} \right) \\ & \quad + \frac{1}{\frac{\bar{h}_{ii}}{\bar{h}_{ji}} + \frac{R_i^{(\kappa)} p_j^{(\kappa)}}{p_i^{(\kappa)}}} \left( \Upsilon_{ij}^{(\kappa)}(\mathbf{R}_i, \mathbf{p}_j) - \frac{R_i^{(\kappa)} p_j^{(\kappa)}}{p_i^{(\kappa)}} \mathbf{p}_i \right). \end{aligned} \quad (48)$$

Initialized from a feasible  $(p^{(0)}, R^{(0)}, r^{(0)})$  for (45) we solve the following convex program at the  $\kappa$ -th iteration to generate the next iterative point  $(p^{(\kappa+1)}, R_i^{(\kappa+1)}, r_u^{(\kappa+1)})$ :

$$\max_{\mathbf{w}, \mathbf{r}} \min_{i=1, \dots, M} [A_i^{(\kappa)}(\mathbf{R}_i) - a_i^{(\kappa)}(\mathbf{r}_i)] \quad (49a)$$

$$\text{s.t.} \quad (4b), (27b), (32), (34b), (44c), (47) \quad (49b)$$

$$\begin{aligned} & \mathbf{p}_i \bar{h}_{ii} [\delta \ln(1 - \epsilon_c) - 1] + \sigma_i^2 \mathbf{R}_i + \sum_{j \neq i} \bar{h}_{ji} \Upsilon_{ij}^{(\kappa)}(\mathbf{R}_i, \mathbf{p}_j) \\ & + \delta \bar{h}_{ii} \sum_{j \neq i}^M \Phi_{ij}^{(\kappa)}(\mathbf{R}_i, \mathbf{p}_j, \mathbf{p}_i) \leq 0, \quad (49c) \\ & i = 1, \dots, M. \end{aligned}$$

The computational complexity of (49) is  $\mathcal{O}((3M)^2(9M)^{2.5} + (9M)^{2.5})$ .

At the same  $\kappa$ -th iteration,  $r_i^{(\kappa+1)}$  is found from solving (35) by bisection on  $[0, r_{u,i}^{(\kappa+1)}]$  such that (36), while  $R_i^{(\kappa+1)}$  is found from solving

$$\zeta_i(\mathbf{R}_i) = 0, i = 1, \dots, M, \quad (50)$$

for the increasing function

$$\begin{aligned} \zeta_i(\mathbf{R}_i) & \triangleq \delta \ln(1 - \epsilon_c) - 1 + \frac{\mathbf{R}_i (\sigma_i^2 + \sum_{j \neq i} \bar{h}_{ji} p_j^{(\kappa+1)})}{\bar{h}_{ii} p_i^{(\kappa+1)}} \\ & \quad + \delta \sum_{j \neq i}^M \ln \left( 1 + \frac{\bar{h}_{ji} \mathbf{R}_i p_j^{(\kappa+1)}}{\bar{h}_{ii} p_i^{(\kappa+1)}} \right), \end{aligned}$$



by bisection on  $[R_{l,i}^{(\kappa+1)}, R_{u,i}]$  with  $\zeta_i(R_{u,i}) > 0$  such that

$$-\epsilon_b \leq g_i(R_i^{(\kappa+1)}) \leq 0. \quad (51)$$

$R_{u,i}$  can be easily located: initialized by  $R_i = 2R_{l,i}^{(\kappa+1)}$  and check  $\zeta_i(R_i)$ . If  $\zeta_i(R_i) > 0$  then we are done. Otherwise reset  $R_i \leftarrow 2R_i$  until  $\zeta_i(R_i) > 0$ . Intuitively, taking  $R_{u,i} = 2\bar{h}_{ii}p_i^{(\kappa+1)}/(\sigma_i^2 + \sum_{j \neq i} \bar{h}_{ji}p_j^{(\kappa+1)})$  will work.

In summary, we propose in Algorithm 3 a path-following computational procedure for the maximin secrecy throughput optimization problem (45), which at least converges to its locally optimal solution satisfying the first order necessary optimality condition.

**Algorithm 3** Path-following algorithm for maximin secrecy throughput optimization

**Initialization:** Set  $\kappa = 0$ . Choose an initial feasible point  $(p^{(0)}, R^{(0)}, r^{(0)})$  for (45) and calculate  $R_{\min}^{(0)}$  as the value of the objective function in (45) at  $(p^{(0)}, R^{(0)}, r^{(0)})$ .

**repeat**

- Set  $\kappa = \kappa + 1$ .
- Solve the convex optimization problem (49) to obtain the solution  $(p^{(\kappa)}, R_i^{(\kappa)}, r_u^{(\kappa)})$ .
- Solve the nonlinear equations (35) to obtain the roots  $r_i^{(\kappa)}$ .
- Solve the nonlinear equations (50) to obtain the roots  $R_i^{(\kappa)}$ .
- Calculate  $R_{\min}^{(\kappa)}$  as the value of the objective function in (45) at  $(p^{(\kappa)}, R^{(\kappa)}, r^{(\kappa)})$ .

**until**  $\frac{R_{\min}^{(\kappa)} - R_{\min}^{(\kappa-1)}}{R_{\min}^{(\kappa-1)}} \leq \epsilon_{\text{tol}}$ .

An initial feasible  $(p^{(0)}, R^{(0)}, r^{(0)})$  can be easily found as follows: taking any  $p^{(0)}$  feasible to the power constraint (4b) to find  $R^{(0)}$  and  $r^{(0)}$  from solving

$$\begin{aligned} \zeta_i(\mathbf{R}_i) &\triangleq \delta \ln(1 - \epsilon_c) - 1 + \frac{\mathbf{R}_i(\sigma_i^2 + \sum_{j \neq i} \bar{h}_{ji}p_j^{(0)})}{\bar{h}_{ii}p_i^{(0)}} \\ &+ \delta \sum_{j \neq i}^M \ln \left( 1 + \frac{\bar{h}_{ji}\mathbf{R}_i p_j^{(0)}}{\bar{h}_{ii}p_i^{(0)}} \right) = 0, i = 1, \dots, M, \end{aligned}$$

by bisection on  $[0, 2\bar{h}_{ii}p_i^{(0)}/(\sigma_i^2 + \sum_{j \neq i} \bar{h}_{ji}p_j^{(0)})]$ , and  $r^{(0)}$  is found from solving

$$\ln(1 - \epsilon_c) + \frac{\mathbf{r}_i \sigma_e^2}{\bar{h}_{ie}p_i^{(0)}} + \sum_{j \neq i}^M \ln \left( 1 + \frac{\mathbf{r}_i \bar{h}_{je}p_j^{(0)}}{\bar{h}_{ie}p_i^{(0)}} \right) = 0, \quad i = 1, \dots, M,$$

by bisection on  $[0, \bar{h}_{ie}p_i^{(0)}/\sigma_e^2]$ .

Lastly, the network secure energy efficiency problem is now formulated by

$$\max_{\mathbf{p}, \mathbf{R}, \mathbf{r}} \quad \frac{\sum_{i=1}^M (\ln(1 + \mathbf{R}_i) - \ln(1 + \mathbf{r}_i))}{\pi(\mathbf{p})} \quad (52a)$$

$$\text{s.t.} \quad (4b), (27b), (28b), (43), (44c), \quad (52b)$$

$$\ln(1 + \mathbf{R}_i) - \ln(1 + \mathbf{r}_i) \geq c_i, \quad (52c)$$

$$i = 1, \dots, M. \quad (52d)$$

To this end, we use inequality (73) in Appendix II to obtain

$$\begin{aligned} \frac{\ln(1 + \mathbf{R}_i)}{\pi(\mathbf{p})} &\geq \tilde{A}_i^{(\kappa)}(\mathbf{R}_i, \mathbf{p}) \\ &\triangleq \frac{2 \ln(1 + R_i^{(\kappa)})}{\pi(p^{(\kappa)})} + \frac{R_i^{(\kappa)}}{\pi(p^{(\kappa)})(1 + R_i^{(\kappa)})} \\ &\times \left( 1 - \frac{R_i^{(\kappa)}}{\mathbf{R}_i} \right) - \frac{\ln(1 + R_i^{(\kappa)})}{\pi^2(p^{(\kappa)})} \pi(\mathbf{p}) \end{aligned} \quad (53)$$

Initialized by a feasible point  $(R^{(0)}, r^{(0)}, p^{(0)})$ , at the  $\kappa$ -th iteration, the following convex program is solved to generate  $(R^{(\kappa+1)}, r^{(\kappa+1)}, p^{(\kappa+1)})$

$$\max_{\mathbf{w}, \mathbf{r}} \quad \sum_{i=1}^M \left[ \tilde{A}_i^{(\kappa)}(\mathbf{R}_i, \mathbf{p}) + \tilde{a}_i^{(\kappa)}(\mathbf{r}_i, \mathbf{p}) \right] \quad (54a)$$

$$\text{s.t.} \quad (4b), (27b), (32), (34b), (44c), (47), (49c), (54b)$$

$$A_i^{(\kappa)}(\mathbf{R}_i) - a_i^{(\kappa)}(\mathbf{r}_i) \geq c_i, \quad i = 1, \dots, M. \quad (54c)$$

The computational complexity of (49) is  $\mathcal{O}((3M)^2(10M)^{2.5} + (10M)^{2.5})$ .

It can be shown that the computational procedure that invokes the convex program (54) to generate the next iterative point, is path-following for (52), which at least converges to its locally optimal solution satisfying the KKT conditions.

A point  $(p^{(0)}, R^{(0)}, r^{(0)})$  is feasible for (52) if and only if  $\min_{i=1, \dots, M} [f_i(R_i^{(0)}) - \ln(1 + r_i^{(0)})]/c_i \geq 1$  and thus can be easily located by adapting Algorithm 3.

Similarly, a path-following procedure for the following maximin SEE optimization problem can be proposed

$$\max_{\mathbf{p}, \mathbf{r}} \quad \min_{i=1, \dots, M} \frac{f_i(\mathbf{R}_i) - \ln(1 + \mathbf{r}_i)}{\pi_i(\mathbf{p})} \quad (55)$$

$$\text{s.t.} \quad (4b), (27b), (28b), (43), (44c), (52c).$$

## V. SIMULATION

This section evaluates the performance of the proposed algorithms through extensive simulation. Considered in all simulation studies is a wireless network with  $M = 10$  transmitter-user communication pairs and noise variance  $\sigma_i^2 = \sigma_e^2 = 1$  mW [34]. All channels among each pair are i.i.d. complex normal random variable with zero mean and unit variance. The drain efficiency of power amplifier  $1/\zeta$  is set to be 40% and the circuit power of each transmitter is  $P_c^i = 5$  mW. Besides, we set  $\epsilon_c = 0.1$  and  $\epsilon_{EV} \in \{0.1, 0.6\}$  and  $\delta = 0.1$ . The computation tolerance for terminating all proposed Algorithms is  $\epsilon_{\text{tol}} = 10^{-4}$ . We divide the obtained information throughput results by  $\ln(2)$  to arrive at the unit of bps/Hz (in throughput) and bits/J/Hz (in energy efficiency).

### A. Maximin secrecy throughput optimization

This subsection analyzes the secrecy throughput in the presence of eavesdropper. In what follows, we consider five cases, including “Perfect CSI”, “Partial CSI ( $\epsilon_{EV} = 0.1$ )”, “Partial CSI ( $\epsilon_{EV} = 0.6$ )”, “Robust Opt. ( $\epsilon_{EV} = 0.1$   $\epsilon_c = 0.1$ )” and “Robust Opt. ( $\epsilon_{EV} = 0.6$   $\epsilon_c = 0.1$ )”. The terms “Perfect CSI”, “Partial CSI” and “Robust Opt.” correspond to the scenarios discussed in Sections III, IV and V, respectively. Fig. 2 plots

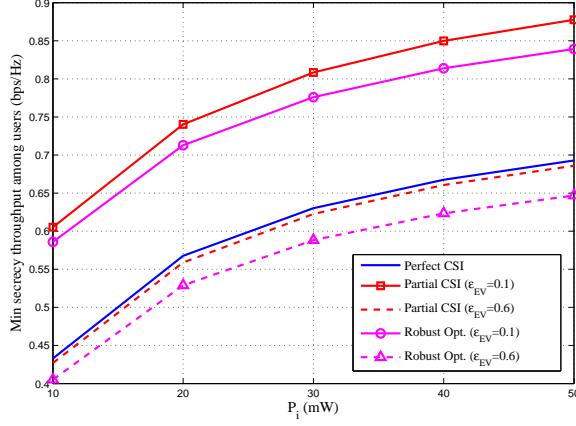


Fig. 2. Min secrecy throughput among users versus the transmit power budget

TABLE I

AVERAGE NUMBER OF ITERATIONS FOR MAXIMIN SECRECY THROUGHPUT OPTIMIZATION.

$P_i$ (mW)	10	20	30	40	50
Perfect CSI	8.12	7.63	7.61	7.71	8.56
Partial CSI ( $\epsilon_{EV} = 0.1$ )	11.25	10.87	10.73	10.40	10.31
Partial CSI ( $\epsilon_{EV} = 0.6$ )	13.12	12.18	14.92	12.60	11.68
Robust Opt. ( $\epsilon_{EV} = 0.1$ )	4.20	4.33	4.20	3.52	3.35
Robust Opt. ( $\epsilon_{EV} = 0.6$ )	5.18	4.96	4.82	4.14	4.90

the minimum secrecy throughput versus the transmit power budget  $P_i$  varying from 10 to 50 mW. As expected, it is seen that the secrecy throughput increase with the transmitted power budget  $P_i$ . It is also observed that the secrecy throughput of “Partial CSI” with  $\epsilon_{EV} = 0.1$  is always better than the secrecy throughputs of others. For  $\epsilon_{EV} = 0.1$ , “Partial CSI” and “Robust Opt.” clearly and significantly outperform “Perfect CSI”. However, the secrecy throughput of “Perfect CSI” is superior to the secrecy throughputs of “Partial CSI” and “Robust Opt.” with  $\epsilon_{EV} = 0.6$ . This is not a surprise because according to the wiretapped throughput defined by (2) and the throughput outage defined by (25)-(26), the former is seen higher than the later for small  $\epsilon_{EV}$ .

Table I provides the average number of iterations required to solve maximin secrecy throughput optimization for the above three cases. As can be observed, our proposed algorithm converges in less than 14 iterations, on average, for all considered cases.

### B. Energy efficiency maximization

In this subsection, we first examine the performance of EE maximization algorithm versus the QoS constraint. The transmitted power  $P_i$  is fixed at 20 mW and QoS constraint  $c_i$  varies from 0.1 to 0.5 bps/Hz. It can be observed from Fig. 3 that the EE performance degrades as the QoS constraint  $c_i$  increases. Moreover, “Partial CSI” with  $\epsilon_{EV} = 0.1$  outperforms others in terms of EE performance. To find out the impact on the sum throughput and total power consumption in EE maximization algorithm, the achieved sum throughput and the total power consumed are illustrated in Fig. 4 and 5, respectively. It can be seen that the total power consumption increases faster

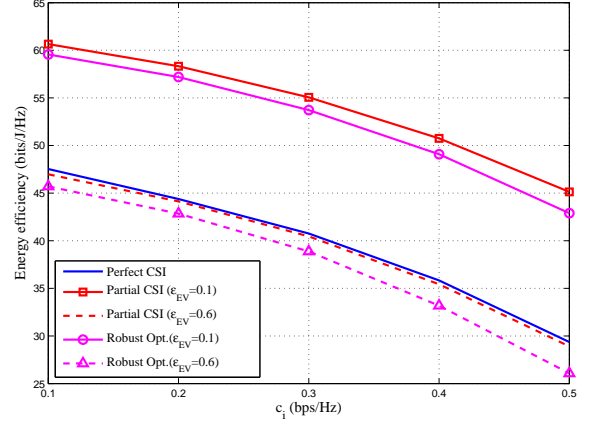


Fig. 3. Energy efficiency versus QoS constraint

TABLE II

AVERAGE NUMBER OF ITERATIONS FOR ENERGY EFFICIENCY MAXIMIZATION.

$c_i$ (bps/Hz)	0.1	0.2	0.3	0.4	0.5
Perfect CSI	32.21	29.62	24.26	21.23	15.33
Partial CSI ( $\epsilon_{EV} = 0.1$ )	33.73	33.12	28.75	25.74	23.25
Partial CSI ( $\epsilon_{EV} = 0.6$ )	35.82	30.56	34.22	22.26	18.34
Robust Opt. ( $\epsilon_{EV} = 0.1$ )	24.25	27.41	25.53	30.06	31.75
Robust Opt. ( $\epsilon_{EV} = 0.6$ )	29.02	23.76	26.80	29.32	23.46

than the sum throughput, which explains why EE degrades as  $c_i$  increases in Fig. 3. Although the sum throughput of “Robust Opt.” is slightly better than “Partial CSI”, “Partial CSI” consumes less power than “Robust Opt.”. Table II shows that our proposed EE maximization algorithm converges in less than 35 iterations, on average, in all considered cases.

Next, we further investigate the performance of EE versus the transmit power budget. The QoS constraint  $c_i$  is fixed at 0.4 bps/Hz and  $P_i$  varies from 10 to 50 mW. As shown in Fig. 6, we observe that the EE performance of “Partial CSI” with  $\epsilon_{EV} = 0.1$  clearly and significantly outperforms the optimized EE of other cases. Furthermore, it can be seen that the EE performances saturate when the transmit power budget exceeds

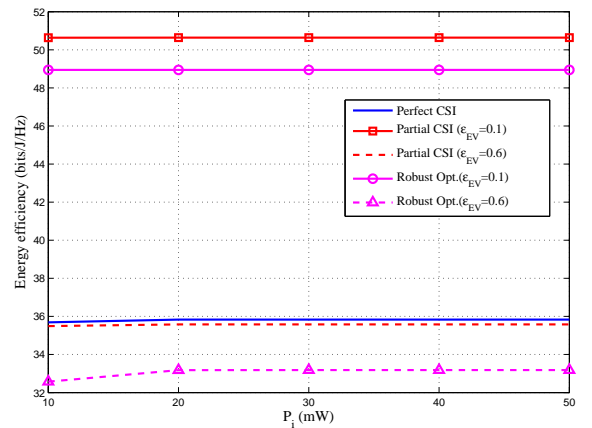


Fig. 6. Energy efficiency versus the transmit power budget

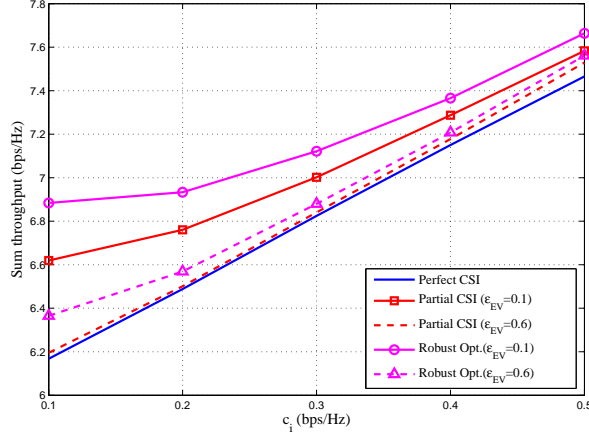


Fig. 4. Sum throughput versus QoS constraint

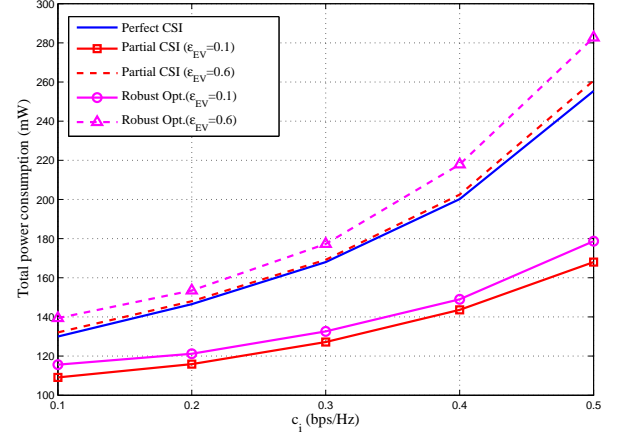


Fig. 5. Total power consumption versus QoS constraint

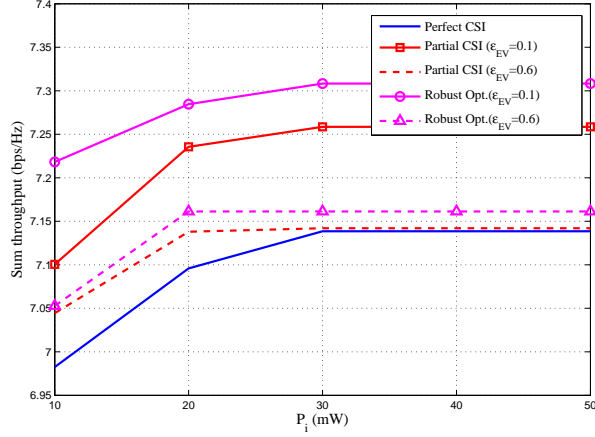


Fig. 7. Sum throughput versus the transmit power budget

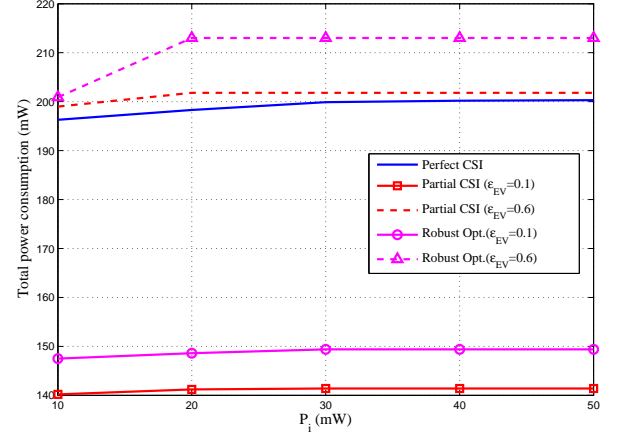


Fig. 8. Total power consumption versus the transmit power budget

the threshold. That is because for small transmit power budget, the denominator of EE is dominated by the circuit power and the EE is maximized by maximization of the sum throughput in the numerator. However, for larger transmit power budget, the denominator of EE is dominated by the actual transmit power. When the total power consumption saturates in Fig. 8, both the EE and the sum throughput accordingly saturate in Figs. 6 and 7.

### C. Maximin energy efficiency optimization

In this subsection, we aim to maximize the minimum EE performance. Firstly, Fig. 9 plots the maximized minimum EE versus QoS constraint. The transmitted power  $P_i$  is fixed at 20 mW and QoS constraint  $c_i$  varies from 0.1 to 0.5 bps/Hz. It can be seen that the optimized minimum EE decreases with increasing  $c_i$  and the EE performance of “Partial CSI” with  $\epsilon_{EV} = 0.1$  is always better than the optimized EE of other cases. Furthermore, it is also observed that for  $\epsilon_{EV} = 0.1$  “Partial CSI” and “Robust Opt.” outperform “Perfect CSI” in terms of EE performance, while “Perfect CSI” is superior to “Partial CSI” and “Robust Opt.” for  $\epsilon_{EV} = 0.6$ . The corresponding throughput and power consumption are plotted

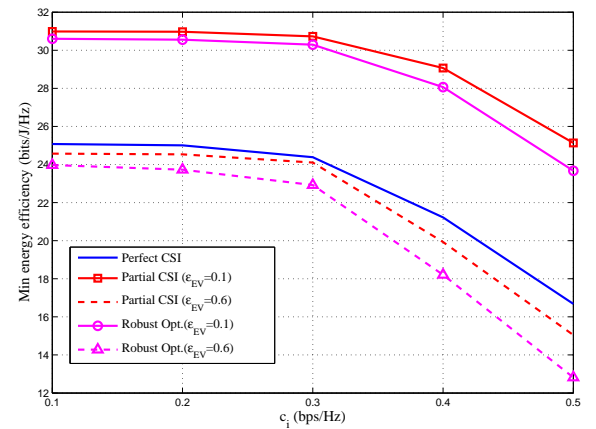


Fig. 9. Minimum energy efficiency versus the QoS constraint

in Fig. 10 and 11, respectively. Table III shows that maximin EE optimization converges in less than 33 iterations, on average, in all considered cases.

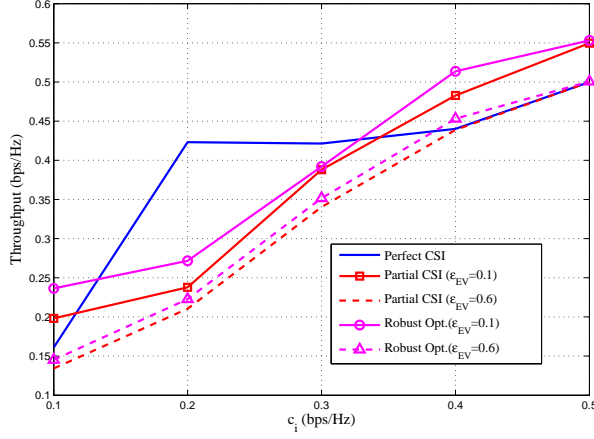


Fig. 10. Throughput versus the QoS constraint

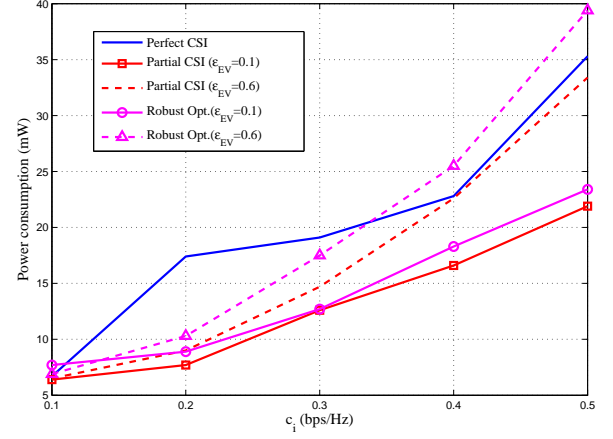


Fig. 11. Power consumption versus the QoS constraint

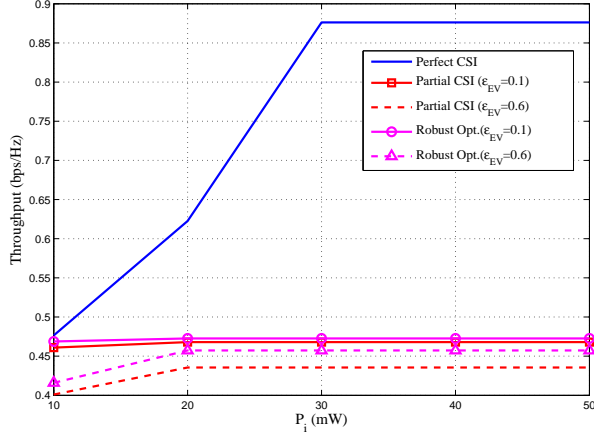


Fig. 13. Throughput versus the transmit power budget

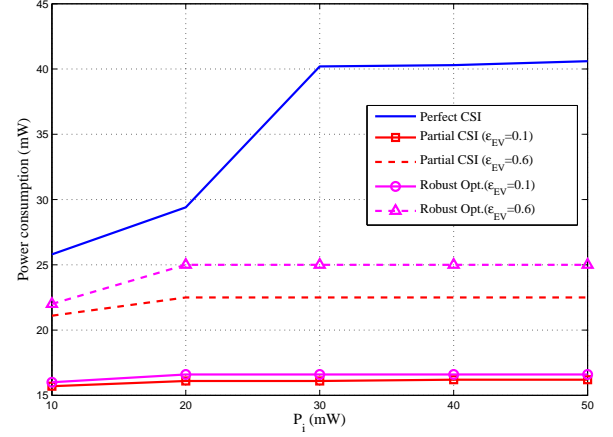


Fig. 14. Power consumption versus the transmit power budget

TABLE III  
AVERAGE NUMBER OF ITERATIONS FOR MAXIMIN ENERGY EFFICIENCY OPTIMIZATION.

$c_i$ (bps/Hz)	0.1	0.2	0.3	0.4	0.5
Perfect CSI	32.42	30.35	31.61	29.23	22.25
Partial CSI ( $\epsilon_{EV} = 0.1$ )	21.86	22.13	20.42	20.82	30.23
Partial CSI ( $\epsilon_{EV} = 0.6$ )	23.66	25.02	22.68	33.30	29.34
Robust Opt. ( $\epsilon_{EV} = 0.1$ )	16.05	23.27	23.36	31.15	18.62
Robust Opt. ( $\epsilon_{EV} = 0.6$ )	20.78	26.12	31.24	27.46	23.92

Next, we investigate the maximin EE performance versus the transmit power budget. The QoS constraint  $c_i$  is fixed at 0.4 bps/Hz and  $P_i$  varies from 10 to 50 mW. The minimum EE performance versus the transmit power budget is illustrated in Fig. 12. Again, we observe that the optimized minimum EE saturates when the transmit power is larger than some threshold. This is due to the fact that under small transmit power regime, the EE is maximized by maximizing the throughput in the numerator. When the transmit power is large enough to obtain the optimized EE, both throughput and power consumption accordingly saturate in Figs. 13 and 14.

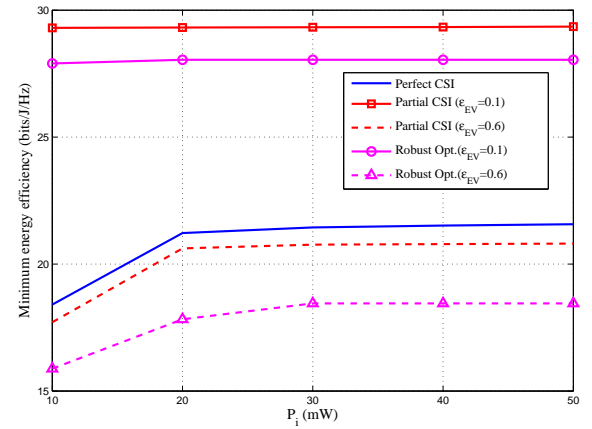


Fig. 12. Minimum energy efficiency versus the transmit power budget

## VI. CONCLUSIONS

We have considered the problem of power allocation to maximize the worst links's secrecy throughput or the network's

secure energy efficiency under various scenarios of available channel state information. We have further proposed path-following algorithms tailored for each of the considered scenarios. Finally, we have provided simulations to show the efficiency of the proposed algorithms. Extensions to beamforming in multi-input single-output (MISO) interference networks with multiple eavesdroppers are under current investigation.

#### APPENDIX I: OUTAGE PROBABILITY FUNDAMENTAL

Recall a probability distribution  $\chi$  is called an *exponential distribution* if its probability density function (pdf) is in form  $\lambda e^{-\lambda x}$  with  $\lambda > 0$ . It is immediate to check that  $\text{Prob}(\chi \geq t) = e^{-\lambda t}$  and  $\mathbb{E}[\chi] = 1/\lambda$ . Recall the following result [29, (15)].

*Theorem 1:* Suppose  $z_1, \dots, z_n$  are independent exponentially distributed random variables with  $\mathbb{E}(z_i) = 1/\lambda_i$ . Then for deterministic  $p_i > 0$ ,  $i = 1, \dots, n$ :

$$\text{Prob}(p_1 z_1 \leq \sum_{i=2}^n p_i z_i) = 1 - \prod_{i=2}^n \frac{1}{1 + (\lambda_1/p_1)/(\lambda_i/p_i)}. \quad (56)$$

It follows from (56) that

$$\begin{aligned} \text{Prob}(p_1 z_1 > c + \sum_{i=2}^n p_i z_i) &= \\ e^{-\lambda_1 c/p_1} \prod_{i=2}^n \frac{1}{1 + (\lambda_1/p_1)/(\lambda_i/p_i)} & \end{aligned} \quad (57)$$

and

$$\begin{aligned} \text{Prob}\left(\frac{p_1 z_1}{\sum_{i=2}^n p_i z_i + \sigma} > \gamma\right) &= \\ \text{Prob}\left(p_1 z_1 > \sum_{i=2}^n \gamma p_i z_i + \gamma \sigma\right) &= \\ e^{-\lambda_1 \gamma \sigma/p_1} \prod_{i=2}^n \frac{1}{1 + \gamma(\lambda_1/p_1)/(\lambda_i/p_i)}. & \end{aligned} \quad (58)$$

Sometimes, it is also more convenient to write (56), (57) and (58) in terms of means  $\bar{\lambda}_i = 1/\lambda_i$  of  $z_i$  as

$$\text{Prob}(p_1 z_1 \leq \sum_{i=2}^n p_i z_i) = 1 - \prod_{i=2}^n \frac{p_1 \bar{\lambda}_1}{p_1 \bar{\lambda}_1 + p_i \bar{\lambda}_i}, \quad (59)$$

$$\text{Prob}(p_1 z_1 > c + \sum_{i=2}^n p_i z_i) = e^{-c/p_1 \bar{\lambda}_1} \prod_{i=2}^n \frac{p_1 \bar{\lambda}_1}{p_1 \bar{\lambda}_1 + p_i \bar{\lambda}_i}, \quad (60)$$

$$\text{Prob}\left(\frac{p_1 z_1}{\sum_{i=2}^n p_i z_i + \sigma} > \gamma\right) = e^{-\gamma \sigma/p_1 \bar{\lambda}_1} \prod_{i=2}^n \frac{p_1 \bar{\lambda}_1}{p_1 \bar{\lambda}_1 + \gamma p_i \bar{\lambda}_i} \quad (61)$$

*Theorem 2:* For given  $\varepsilon > 0$ , define

$$r_{\max} \triangleq \max\{r : \text{Prob}\left(\frac{p_1 z_1}{\sum_{i=2}^n p_i z_i + \sigma^2} < r\right) \leq \varepsilon\} \quad (62)$$

Then  $r_{\max}$  is the unique positive root of the nonlinear equation

$$\ln(1 - \varepsilon) + \frac{r \sigma^2}{p_1 \bar{\lambda}_1} + \sum_{i=2}^n \ln\left(1 + \frac{r p_i \bar{\lambda}_i}{p_1 \bar{\lambda}_1}\right) = 0. \quad (63)$$

*Proof:* Applying (60) yields

$$\begin{aligned} \text{Prob}\left(\frac{p_1 z_1}{\sum_{i=2}^n p_i z_i + \sigma^2} < r\right) &= \\ \text{Prob}(p_1 z_1 < r(\sum_{i=2}^n p_i z_i + \sigma^2)) &= \\ 1 - e^{-r \sigma^2/p_1 \bar{\lambda}_1} \prod_{i=2}^n \frac{p_1 \bar{\lambda}_1}{p_1 \bar{\lambda}_1 + r p_i \bar{\lambda}_i}. & \end{aligned} \quad (64)$$

Therefore,

$$\begin{aligned} \text{Prob}\left(\frac{p_1 z_1}{\sum_{i=2}^n p_i z_i + \sigma^2} < r\right) &\leq \varepsilon \\ \Leftrightarrow 1 - e^{-r \sigma^2/p_1 \bar{\lambda}_1} \prod_{i=2}^n \frac{p_1 \bar{\lambda}_1}{p_1 \bar{\lambda}_1 + r p_i \bar{\lambda}_i} &\leq \varepsilon \\ \Leftrightarrow \ln(1 - \varepsilon) + \frac{r \sigma^2}{p_1 \bar{\lambda}_1} + \sum_{i=2}^n \ln\left(1 + \frac{r p_i \bar{\lambda}_i}{p_1 \bar{\lambda}_1}\right) &\leq 0. \end{aligned} \quad (65)$$

By noticing that the function in the left hand side (LHS) of (65) is increasing in  $r$ , we arrive at (63).  $\square$

*Theorem 3:* Suppose  $\bar{z}_i > 0$ ,  $p_i > 0$ ,  $\delta > 0$  and  $\sigma > 0$  are deterministic values, while  $\tilde{z}_i$  are independent exponential distributions. For  $\varepsilon > 0$ , define

$$r_p \triangleq \max\{r : \text{Prob}\left(\frac{p_1 \bar{z}_1(1 + \delta \tilde{z}_1)}{\sum_{i=2}^n p_i \bar{z}_i(1 + \delta \tilde{z}_i) + \sigma^2} < r\right) \leq \varepsilon\}. \quad (66)$$

Then  $r_p$  is the unique positive root of the nonlinear equation

$$\begin{aligned} \delta \ln(1 - \varepsilon) + \frac{r(\sigma^2 + \sum_{i=2}^n p_i \bar{z}_i) - p_1 \bar{z}_1}{\bar{z}_1 p_1} \\ + \delta \sum_{i=2}^n \ln\left(1 + \frac{r \bar{z}_i p_i}{\bar{z}_1 p_1}\right) = 0. \end{aligned} \quad (67)$$

*Proof:* Using (65) yields

$$\begin{aligned} \text{Prob}\left(\frac{p_1 \bar{z}_1(1 + \delta \tilde{z}_1)}{\sum_{i=2}^n p_i \bar{z}_i(1 + \delta \tilde{z}_i) + \sigma^2} < r\right) &\leq \varepsilon \\ \Leftrightarrow \ln(1 - \varepsilon) + \frac{r(\sigma^2 + \sum_{i=2}^n p_i \bar{z}_i) - p_1 \bar{z}_1}{\bar{z}_1 p_1 \delta} \\ + \sum_{i=2}^n \ln\left(1 + \frac{r \bar{z}_i p_i}{\bar{z}_1 p_1}\right) &\leq 0 \\ \Leftrightarrow \delta \ln(1 - \varepsilon) + \frac{r(\sigma^2 + \sum_{i=2}^n p_i \bar{z}_i) - p_1 \bar{z}_1}{\bar{z}_1 p_1} \\ + \delta \sum_{i=2}^n \ln\left(1 + \frac{r \bar{z}_i p_i}{\bar{z}_1 p_1}\right) &\leq 0. \end{aligned} \quad (68)$$

Again, by noticing that the function in the LHS of (69) is increasing in  $r$  we arrive at (67).  $\square$

One can see that for  $\delta \rightarrow 0$  (less uncertainty), (69) becomes

$$\begin{aligned} \frac{r(\sigma^2 + \sum_{i=2}^n p_i \bar{z}_i) - p_1 \bar{z}_1}{\bar{z}_1 p_1} &\leq 0 \\ \Leftrightarrow r(\sigma^2 + \sum_{i=2}^n p_i \bar{z}_i) - p_1 \bar{z}_1 &\leq 0 \\ \Leftrightarrow r &\leq \frac{p_1 \bar{z}_1}{\sigma^2 + \sum_{i=2}^n p_i \bar{z}_i}, \end{aligned}$$

so  $r_p$  is the standard ratio

$$\frac{p_1 \bar{z}_1}{\sigma^2 + \sum_{i=2}^n p_i \bar{z}_i}.$$

## APPENDIX II: FUNDAMENTAL INEQUALITIES

*Lemma 1:* It is true that

$$\ln(1 + 1/t) \geq 1/(t+1) \quad \forall t > 0 \quad (70)$$

*Proof:* One can easily check  $(t+1) \ln(1+1/t) \geq 1 \quad \forall t > 0$  by plotting the graph of function  $(t+1) \ln(1+1/t)$  over  $(0, +\infty)$ .  $\square$

*Theorem 4:* The function  $f(x, y, t) \triangleq \ln(1 + 1/xy)^{1/t}$  is convex in the domain  $\{x > 0, y > 0, t > 0\}$ .

*Proof:* Writing  $f(x, y, t) = (1/t)(\ln(xy+1) - \ln x - \ln y)$ , it is ease to see that the Hessian  $\nabla^2 f(x, y, t)$  is

$$\begin{aligned} \nabla^2 f(x, y, t) &= \begin{bmatrix} \frac{2xy+1}{x^2(xy+1)^2t} & \frac{1}{(xy+1)^2t} & \frac{1}{t^2(xy+1)x} \\ \frac{1}{(xy+1)^2t} & \frac{1}{y^2(xy+1)^2t} & \frac{1}{t^2(xy+1)y} \\ \frac{1}{t^2(xy+1)x} & \frac{1}{t^2(xy+1)y} & \frac{2 \ln(1+1/xy)}{t^3} \end{bmatrix} \\ &\succeq \begin{bmatrix} \frac{2xy+1}{x^2(xy+1)^2t} & \frac{1}{(xy+1)^2t} & \frac{1}{t^2(xy+1)x} \\ \frac{1}{(xy+1)^2t} & \frac{1}{y^2(xy+1)^2t} & \frac{1}{t^2(xy+1)y} \\ \frac{1}{t^2(xy+1)x} & \frac{1}{t^2(xy+1)y} & \frac{2 \ln(1+1/xy)}{t^3} \end{bmatrix} \\ &\quad (x^2y^2(xy+1)^2t^3)^{-1} \\ &\quad \cdot \begin{bmatrix} (xy+1)y^2t^2 & x^2y^2t^2 & t(xy+1)xy^2 \\ x^2y^2t^2 & (xy+1)x^2t^2 & t(xy+1)x^2y \\ t(xy+1)xy^2 & t(xy+1)x^2y & 2(xy+1)x^2y^2 \end{bmatrix}, \quad (71) \end{aligned}$$

where the inequality (70) has been applied to the  $(3, 3)$ -th entry of  $\nabla^2 f(x, y, t)$  to arrive the matrix inequality in (71). Here and after,  $\mathcal{A} \succeq \mathcal{B}$  for matrices  $\mathcal{A}$  and  $\mathcal{B}$  means that  $\mathcal{A} - \mathcal{B}$  is a positive definite matrix. Then, calculating the subdeterminants of matrix in the right hand side (RHS) of (71) yields  $(xy+1)y^2t^2 > 0$ ,

$$\begin{vmatrix} \frac{1}{x^2(xy+1)t} & \frac{1}{(xy+1)^2t} \\ \frac{1}{(xy+1)^2t} & \frac{1}{y^2(xy+1)t} \end{vmatrix} = x^2y^2t^4(2xy+1) > 0$$

and

$$\begin{vmatrix} (xy+1)y^2t^2 & x^2y^2t^2 & t(xy+1)xy^2 \\ x^2y^2t^2 & (xy+1)x^2t^2 & t(xy+1)x^2y \\ t(xy+1)xy^2 & t(xy+1)x^2y & 2(xy+1)x^2y^2 \end{vmatrix} = x^4y^4t^4(xy+1)[(xy+1)^3 - 1] > 0.$$

Therefore the matrix in the RHS of (71) is positive definite, implying that the Hessian  $\nabla^2 f(x, y, t)$  is positive definite, which is the necessary and sufficient condition for the convexity of  $f$  [25].  $\square$

As the function  $f(x, y) \triangleq \ln(1 + 1/xy)$  is convex in the domain  $\{x > 0, y > 0\}$  it follows that [25] for every  $x > 0$ ,  $y > 0$ ,  $\bar{x} > 0$  and  $\bar{y} > 0$ ,

$$\begin{aligned} \ln(1 + 1/xy) &= f(x, y) \\ &\geq f(\bar{x}, \bar{y}) + \langle \nabla f(\bar{x}, \bar{y}), (x, y) - (\bar{x}, \bar{y}) \rangle \\ &= \ln(1 + 1/\bar{x}\bar{y}) \\ &\quad + \frac{1/\bar{x}\bar{y}}{1 + 1/\bar{x}\bar{y}}(2 - x/\bar{x} - y/\bar{y}). \quad (72) \end{aligned}$$

Similarly, for the convex function  $f(x, y, t) \triangleq \ln(1 + 1/xy)^{1/t}$ , one has the following inequality for every  $x > 0$ ,  $y > 0$ ,  $t > 0$ ,  $\bar{x} > 0$ ,  $\bar{y} > 0$  and  $\bar{t} > 0$ ,

$$\begin{aligned} \frac{\ln(1 + 1/xy)}{t} &= f(x, y, t) \\ &\geq f(\bar{x}, \bar{y}, \bar{t}) + \langle \nabla f(\bar{x}, \bar{y}, \bar{t}), (x, y, t) - (\bar{x}, \bar{y}, \bar{t}) \rangle \\ &= \frac{2 \ln(1 + 1/\bar{x}\bar{y})}{\bar{t}} + \frac{1/\bar{x}\bar{y}}{\bar{t}(1 + 1/\bar{x}\bar{y})}(2 \\ &\quad - x/\bar{x} - y/\bar{y}) - \frac{\ln(1 + 1/\bar{x}\bar{y})}{\bar{t}^2}t \quad (73) \end{aligned}$$

Analogously, the inequality

$$\begin{aligned} \frac{-\ln(1+x)}{t} &\geq 2 \frac{\alpha - \ln(1+\bar{x})}{\bar{t}} + \frac{\bar{x}}{\bar{t}(1+\bar{x})} \\ &\quad - \frac{x}{\bar{t}(1+\bar{x})} - \frac{\alpha - \ln(1+\bar{x})}{\bar{t}^2}t - \frac{\alpha}{t} \quad (74) \\ &\quad \forall 0 \leq x \leq M, \alpha \geq \ln(1+M) + 0.5 \end{aligned}$$

follows from the convexity of function  $\frac{\alpha - \ln(1+x)}{t}$  over the trust region  $0 \leq x \leq M$ .

Lastly, the inequality

$$\ln(1+x/y) \leq \ln(1+\bar{x}/\bar{y}) + \frac{1}{1+\bar{x}/\bar{y}}(0.5(x^2/\bar{x}+\bar{x})/y - \bar{x}/\bar{y}) \quad (75)$$

follows from the concavity of function  $\ln(1+z)$  and then the inequality

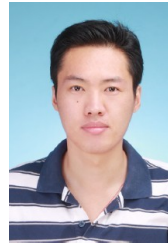
$$\begin{aligned} x &= 0.5(x^2/\bar{x} + \bar{x}) - 0.5(x - \bar{x})^2/\bar{x} \\ &\leq 0.5(x^2/\bar{x} + \bar{x}) \quad \forall x > 0, \bar{x} > 0. \quad (76) \end{aligned}$$

## REFERENCES

- [1] A. G. Fragkiadakis, E. Z. Tragou, and I. G. Askoxyllakis, "A survey on security threats and detection techniques in cognitive radio networks," *IEEE Commun. Surveys Tuts.*, vol. 15, pp. 428–445, Jan 2013.
- [2] A. Mukherjee, S. A. A. Fakoorian, J. Huang, and A. L. Swindlehurst, "Principles of physical layer security in multiuser wireless networks: A survey," *IEEE Commun. Surveys Tuts.*, vol. 16, p. 15501573, Feb 2014.
- [3] Y. Liang, H. V. Poor, and S. Shamai, "Secure communication over fading channels," *IEEE Trans. Inf. Theory*, vol. 54, pp. 2470–2492, June 2008.
- [4] R. Bassily et al, "Cooperative security at the physical layer: A summary of recent advances," *IEEE Signal Process. Mag.*, vol. 30, pp. 16–28, May 2013.
- [5] H. V. Poor, "Information and inference in the wireless physical layer," *IEEE Commun. Mag.*, vol. 19, pp. 40–47, Feb. 2012.
- [6] H. V. Poor and R. F. Schaefer, "Wireless physical layer security," *Proc. of the National Academy of Sciences of the USA*, vol. 114, pp. 19–26, Jan. 2017.
- [7] D. Wang, B. Bai, W. Chen, and Z. Han, "Achieving high energy efficiency and physical-layer security in AF relaying," *IEEE Trans. Wireless Commun.*, vol. 15, pp. 740–752, Jan 2016.
- [8] N. T. Nghia, H. D. Tuan, T. Q. Duong, and H. V. Poor, "MIMO beamforming for secure and energy-efficient wireless communication," *IEEE Signal Process. Lett.*, vol. 24, no. 2, pp. 236–239, 2017.
- [9] L. Dong, Z. Han, A. P. Petropulu, and H. V. Poor, "Improving wireless physical layer security via cooperating relays," *IEEE Trans. Signal Process.*, vol. 58, pp. 1875–1888, Mar. 2010.
- [10] J. Li, A. P. Petropulu, and S. Weber, "On cooperative relaying schemes for wireless physical layer security," *IEEE Trans. Signal Process.*, vol. 59, pp. 4985–4997, Oct. 2011.
- [11] T. M. Hoang, T. Q. Duong, H. A. Suraweera, C. Tellambura, and H. V. Poor, "Cooperative beamforming and user selection for improving the security of relay-aided systems," *IEEE Trans. Commun.*, vol. 63, pp. 5039–5051, Dec. 2015.



- [12] Y. Li, M. Sheng, C. Yang, and X. Wang, "Energy efficiency and spectral efficiency tradeoff in interference-limited wireless networks," *IEEE Commun. Lett.*, vol. 17, pp. 1924–1927, October 2013.
- [13] J. Rostampoor, S. M. Razavizadeh, and I. Lee, "Energy efficiency maximization precoding design for SWIPT in MIMO two-way relay networks," *IEEE Trans. Vehicular Technology*, vol. PP, no. 99, pp. 1–1, 2017.
- [14] M. Zheng, L. Chen, W. Liang, H. Yu, and J. Wu, "Energy-efficiency maximization for cooperative spectrum sensing in cognitive sensor networks," *IEEE Trans. Green Commun. and Networking*, vol. PP, no. 99, pp. 1–1, 2017.
- [15] D. Wang, B. Bai, W. Chen, and Z. Han, "Energy efficient secure communication over decode-and-forward relay channels," *IEEE Trans. Commun.*, vol. 63, pp. 892–905, March 2015.
- [16] J. Farhat, G. Brante, R. D. Souza, and J. L. Rebelatto, "Secure energy efficiency of selective decode and forward with distributed power allocation," in *Proc IEEE Int'l. Symp. on Wireless Communication Systems (ISWCS)*, pp. 701–705, Aug 2015.
- [17] Y. Chen, L. Wang, M. Ma, and B. Jiao, "Power allocation for full-duplex relay networks: Secure energy efficiency optimization," in *Proc IEEE Globecom*, pp. 1–6, Dec 2016.
- [18] X. Xu, W. Yang, Y. Cai, and S. Jin, "On the secure spectral-energy efficiency tradeoff in random cognitive radio networks," *IEEE Journal on Selected Areas in Commun.*, vol. 34, pp. 2706–2722, Oct 2016.
- [19] J. Ouyang, M. Lin, Y. Zou, W. P. Zhu, and D. Massicotte, "Secrecy energy efficiency maximization in cognitive radio networks," *IEEE Access*, vol. 5, pp. 2641–2650, 2017.
- [20] T. T. Vu, H. H. Kha, and H. D. Tuan, "Transceiver design for optimizing the energy efficiency in multiuser MIMO channels," *IEEE Commun. Lett.*, vol. 20, pp. 1507–1510, Aug 2016.
- [21] J. Zheng et al., "Optimal power control in ultra-dense small cell networks: A game-theoretic approach," *IEEE Trans. Wirel. Commun.*, vol. 16, pp. 4139–4150, Jul. 2017.
- [22] G. Zheng, I. Krikidis, C. Masouros, S. Timotheou, D. A. Toumpakaris, and Z. Ding, "Rethinking the role of interference in wireless networks," *IEEE Commun. Mag.*, vol. 52, pp. 152–158, Nov 2014.
- [23] A. Chorti, S. M. Perlaza, Z. Han, and H. V. Poor, "On the resilience of wireless multiuser networks to passive and active eavesdroppers," *IEEE J. Sel. Areas. Commun.*, vol. 31, no. 9, pp. 1850–1863, 2013.
- [24] H. H. Kha, H. D. Tuan, and H. H. Nguyen, "Fast global optimal power allocation in wireless networks by local d.c. programming," *IEEE Trans. Wireless Commun.*, vol. 11, pp. 510–515, Feb. 2012.
- [25] H. Tuy, *Convex Analysis and Global Optimization (second edition)*. Springer, 2017.
- [26] A. A. Nasir, H. D. Tuan, T. Q. Duong, and H. V. Poor, "Secrecy rate beamforming for multicell networks with information and energy harvesting," *IEEE Trans. Signal Process.*, vol. 65, pp. 677–689, Feb. 2017.
- [27] H. H. M. Tam, H. D. Tuan, D. T. Ngo, T. Q. Duong, and H. V. Poor, "Joint load balancing and interference management for small-cell heterogeneous networks with limited backhaul capacity," *IEEE Trans. Wirel. Commun.*, vol. 16, pp. 872–884, Feb. 2017.
- [28] B. R. Marks and G. P. Wright, "A general inner approximation algorithm for nonconvex mathematical programs," *Operation Research*, vol. 26, no. 4, pp. 681–683, 1978.
- [29] S. Kandukuri and S. Boyd, "Optimal power control in interference-limited fading wireless channels with outage-probability specifications," *IEEE Trans. Wireless Commun.*, vol. 1, pp. 46–55, Jan. 2002.
- [30] S. Ghosh, B. D. Rao, and J. R. Zeidler, "Outage-efficient strategies for multi-user MIMO networks with channel distribution information," *IEEE Trans. Signal Process.*, vol. 58, pp. 6312–6324, Dec. 2010.
- [31] W. Li, T. Chang, C. Lin, and C. Chi, "Coordinated beamforming for multiuser MISO interference channel under rate outage constraints," *IEEE Trans. Signal Process.*, vol. 61, pp. 1087–1102, Mar. 2013.
- [32] W. Li, T. Chang, and C. Chi, "Multi-cell coordinated beamforming with rate outage constraint-part I: complexity analysis," *IEEE Trans. Signal Process.*, vol. 63, pp. 2749–2762, Jun. 2015.
- [33] W. Li, T. Chang, and C. Chi, "Multi-cell coordinated beamforming with rate outage constraint-part II: efficient approximation algorithms," *IEEE Trans. Signal Process.*, vol. 63, pp. 2763–2778, Jun. 2015.
- [34] C. Wang, H.-M. Wang, D. W. K. Ng, X.-G. Xia, and C. Liu, "Joint beamforming and power allocation for secrecy in peer-to-peer relay networks," *IEEE Trans. Wireless Commun.*, vol. 14, pp. 3280–3293, June 2015.



wireless communication and signal processing.



Telecommunications, University of New South Wales, from 2003 to 2011. He is currently a Professor with the Faculty of Engineering and Information Technology, University of Technology Sydney. He has been involved in research with the areas of optimization, control, signal processing, wireless communication, and biomedical engineering for more than 20 years.



2012–2015. His research interests are in the area of signal processing in wireless communication systems. He is an Associate Editor for IEEE Canadian Journal of Electrical and Computer Engineering.



(165 articles) and presented at international conferences (125 papers).

Dr. Duong currently serves as an Editor for the IEEE TRANSACTIONS ON WIRELESS COMMUNICATIONS, IEEE TRANSACTIONS ON COMMUNICATIONS, IET COMMUNICATIONS, and a Lead Senior Editor for IEEE COMMUNICATIONS LETTERS. He was awarded the Best Paper Award at the IEEE Vehicular Technology Conference (VTC-Spring) in 2013, IEEE International Conference on Communications (ICC) 2014, IEEE Global Communications Conference (GLOBECOM) 2016, and IEEE Digital Signal Processing Conference (DSP) 2017. He is the recipient of prestigious Royal Academy of Engineering Research Fellowship (2016–2021) and has won a prestigious Newton Prize 2017.

**Zhichao Sheng** was born in Yangzhou, China. He received the B.S. degree in communication engineering from Nanjing University of Information Science and Technology, Nanjing, China, in 2008, the M.S. degree in signal and information processing from Jiangsu University of Science and Technology, Zhenjiang, China, in 2012. He is currently completing the dual-doctoral degree with the University of Technology Sydney, Ultimo, NSW, Australia, and with Shanghai University, Shanghai, China. His research interests include optimization methods for

**Hoang Duong Tuan** received the Diploma (Hons.) and Ph.D. degrees in applied mathematics from Odessa State University, Ukraine, in 1987 and 1991, respectively. He spent nine academic years in Japan as an Assistant Professor in the Department of Electronic-Mechanical Engineering, Nagoya University, from 1994 to 1999, and then as an Associate Professor in the Department of Electrical and Computer Engineering, Toyota Technological Institute, Nagoya, from 1999 to 2003. He was a Professor with the School of Electrical Engineering and

**Ali Arshad Nasir** (S'09-M'13) is an Assistant Professor in the Department of Electrical Engineering, King Fahd University of Petroleum and Minerals (KFUPM), Dhahran, KSA. Previously, he held the position of Assistant Professor in the School of Electrical Engineering and Computer Science (SEECs) at National University of Sciences & Technology (NUST), Pakistan, from 2015–2016. He received his Ph.D. in telecommunications engineering from the Australian National University (ANU), Australia in 2013 and worked there as a Research Fellow from

**Trung Q. Duong** (S'05, M'12, SM'13) received his Ph.D. degree in Telecommunications Systems from Blekinge Institute of Technology (BTH), Sweden in 2012. Currently, he is with Queen's University Belfast (UK), where he was a Lecturer (Assistant Professor) from 2013 to 2017 and a Reader (Associate Professor) from 2018. His current research interests include Internet of Things (IoT), wireless communications, molecular communications, and signal processing. He is the author or co-author of 290 technical papers published in scientific journals



**H. Vincent Poor** (S72, M77, SM82, F87) received the Ph.D. degree in EECS from Princeton University in 1977. From 1977 until 1990, he was on the faculty of the University of Illinois at Urbana-Champaign. Since 1990 he has been on the faculty at Princeton, where he is currently the Michael Henry Strater University Professor of Electrical Engineering. During 2006 to 2016, he served as Dean of Princeton's School of Engineering and Applied Science. He has also held visiting appointments at several other universities, including most recently at Berkeley and

Cambridge. His research interests are in the areas of information theory and signal processing, and their applications in wireless networks, energy systems and related fields. Among his publications in these areas is the recent book *Information Theoretic Security and Privacy of Information Systems* (Cambridge University Press, 2017).

Dr. Poor is a member of the National Academy of Engineering and the National Academy of Sciences, and is a foreign member of the Chinese Academy of Sciences, the Royal Society, and other national and international academies. He received the Marconi and Armstrong Awards of the IEEE Communications Society in 2007 and 2009, respectively. Recent recognition of his work includes the 2017 IEEE Alexander Graham Bell Medal, Honorary Professorships at Peking University and Tsinghua University, both conferred in 2017, and a D.Sc. *honoris causa* from Syracuse University also awarded in 2017.